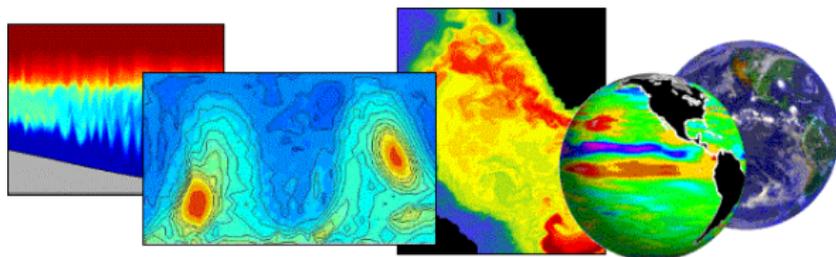


MITgcm formulation improvement



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1. Formulation improvement

- ▶ TEOS-10
- ▶ Anelastic and non-Boussinesq
- ▶ Latent heat
- ▶ Quasi-Hydrostatic

2. Fluid exchange and Energy Reference Level

- ▶ heat budget
- ▶ Run-Off scheme

MITgcm formulation

1. TEOS-10

- ▶ more accurate
- ▶ incorporate variation of C_p into "Conservative Temperature" (CT).

Since we have never considered variation of C_p , using TEOS-10 and CT is the only way to be consistent with constant C_p .

Same regarding absolute salinity (since salinity has always been considered as total amount of salt and not directly related to conductivity).

- ▶ Issue: In Boussinesq model, the Heat budget is computed using the constant (Boussinesq) density ρ_0 . And variation of density are larger than variation of C_p , and in opposite direction.
→ the product $\rho \times C_p$ varies less than ρ alone (true for pressure effect and salinity effect). So, in Boussinesq model, using TEOS-10 is not making the heat-content more consistent.

MITgcm formulation

2. EOS p-dependence in Boussinesq formulation

- ▶ using directly $\rho(T, S, p)$ to integrate hydrostatic pressure is not recommended (in MITgcm, *selectP_in EOS_Zc = 2* or *eosType='JMD95P'*)
- ▶ the case of external gravity wave in homogeneous ocean: compressibility leads to artificial mass source and sink that amplified surface pressure anomaly at depth leading to an increase of the pressure gradient term at depth (\rightarrow no longer barotropic).
- ▶ should use instead: $\rho(T, S, p(z))$
- ▶ current default: $p(z) = -\rho_0 g z$ is a crude approximation
- ▶ better to use: $p(z) = \int g\rho(T_{ref}, S_{ref}, p(z))dz$ with *selectP_in EOS_Zc = 1*

MITgcm formulation

3. Anelastic formulation

- ▶ account for the large part (all deep-water) of density variations
→ more precise heat-budget with TEOS-10
- ▶ but still ignore significant density changes in coastal water
(e.g., near river mouth)

4. Non-Boussinesq formulation using pressure or mass vertical-coordinate

- ▶ would make heat-budget fully consistent when using TEOS-10
- ▶ tried a long time-ago (Losch et al, 2004) but without r^* nor GM
- ▶ recently made to work with few important pkgs (gmredi, gg190)
(use "reasonable" assumption for conversion factor in parameterization)
- ▶ issue with direct comparison of diagnostic η field with SSH observation and with slope term (i.e., $\nabla\eta$) in seaice dynamics

MITgcm formulation

5. Latent heat

should account for temperature variation of latent-heat:

- ▶ linear relation would be consistent with constant C_p for seawater and water vapor $L_v(T) = L_v^o + (C_p^v - C_p^{sw}) * T$
- ▶ constant L_v assumes seawater and water vapor have identical C_p (however C_p^v is less than half of C_p^{sw})

6. Quasi-Hydrostatic formulation to account for $f' = 2\Omega \cos(\phi)$

- ▶ negligible effects reported in Marshall *etal* 97a paper. However, this was before CVS repository; and a bug was found in early CVS repos versions.
- ▶ llc90 has better resolution near equator and near the surface
- ▶ QH AB time-stepping is now fixed (PR #433, was missing for staggered time-step)

Using ERL in MITgcm

Fluid exchange and Energy Reference Level (ERL):

How to account for temperature (heat) forcing and any tracer forcing anytime fluid is added or remove at the surface — primarily run-off, precipitation and evaporation but also freezing and melting — or at depth using *addMass* field.

1. From experience gained with coupled model, it's easier to define an ERL (e.g., liquid water at $0^{\circ}C$) and any departure from the ERL is accounted for in the net heat-flux (sort of "advective" heat flux or a modified latent heat flux).
2. In MITgcm, setting *temp_EvPrRn* (e.g., $= 0^{\circ}C$) defined the ERL. Note: this is the default for any other tracer but not for Temp. with "unset" default, i.e., assuming exchange at the local temperature.
3. The ERL is needed to do a heat-budget when fluid is exchanged (with *useRealFreshWaterFlux* and *Non-Lin Free-Surf*); but using it in the model formulation greatly simplify the heat budget estimation: everything is in the net heat flux.

Using ERL in MITgcm

4. This is a small component of the heat-flux (few W/m^2 , more Evap over warmer SST and precip over colder SST) but comparable to GHG perturbation and larger than, in the atmosphere, the conversion term $PE \rightarrow KE$ and heating due to dissipation.
5. Useful also with other components. Otherwise, to close the budget, needs to track the local temperature precisely when fluid is added/removed (many additional terms added in *seaiice_growth.F* just for this reason).
6. Easier for run-off routing: if 2 rivers merge or flow in same grid-cell, just add the rivers flow, the advective heat-flux and any tracer flux all the same way (no need to compute a "flow weighted" temp).
7. Implementation detail: with (default) synchronous time-stepping, the fluid addition/removal is delayed by 1 time-step vs heat and salt forcing, for consistency between model thickness factor (*hFac*) update and divergence of advective velocity field. In MITgcm, we choose to preserve the exact tracer conservation and tolerate a one time-step mis-match in fresh-water "advective" heat flux addition when using synchronous time-stepping.

Summary

Model formulation improvements

1. TEOS-10 : caution in Boussinesq model
2. EOS p-dependence in Boussinesq formulation
3. Anelastic formulation: account for most Boussinesq inaccuracy
4. Non-Boussinesq formulation using pressure or mass vertical-coordinate
5. Latent heat: fct of SST
6. Quasi-Hydrostatic : minor improvement ?
7. Use Energy Reference Level (ERL): simpler