

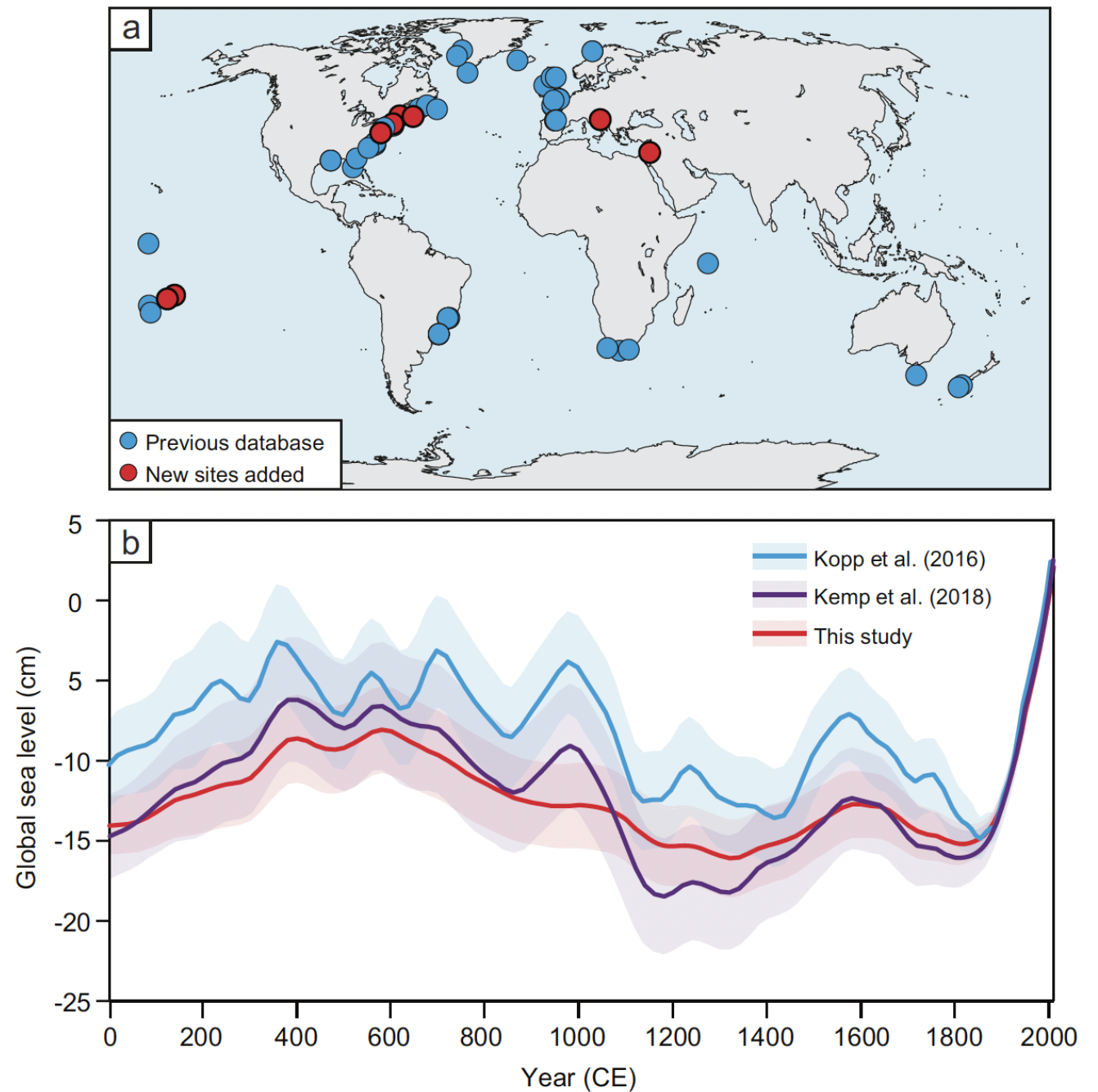
(scattered thoughts on) Sea Level Rise

Christopher Piecuch (WHOI)
2025 ECCO Summer School

**Current rates of sea-level rise are exceptional in
a longterm context**

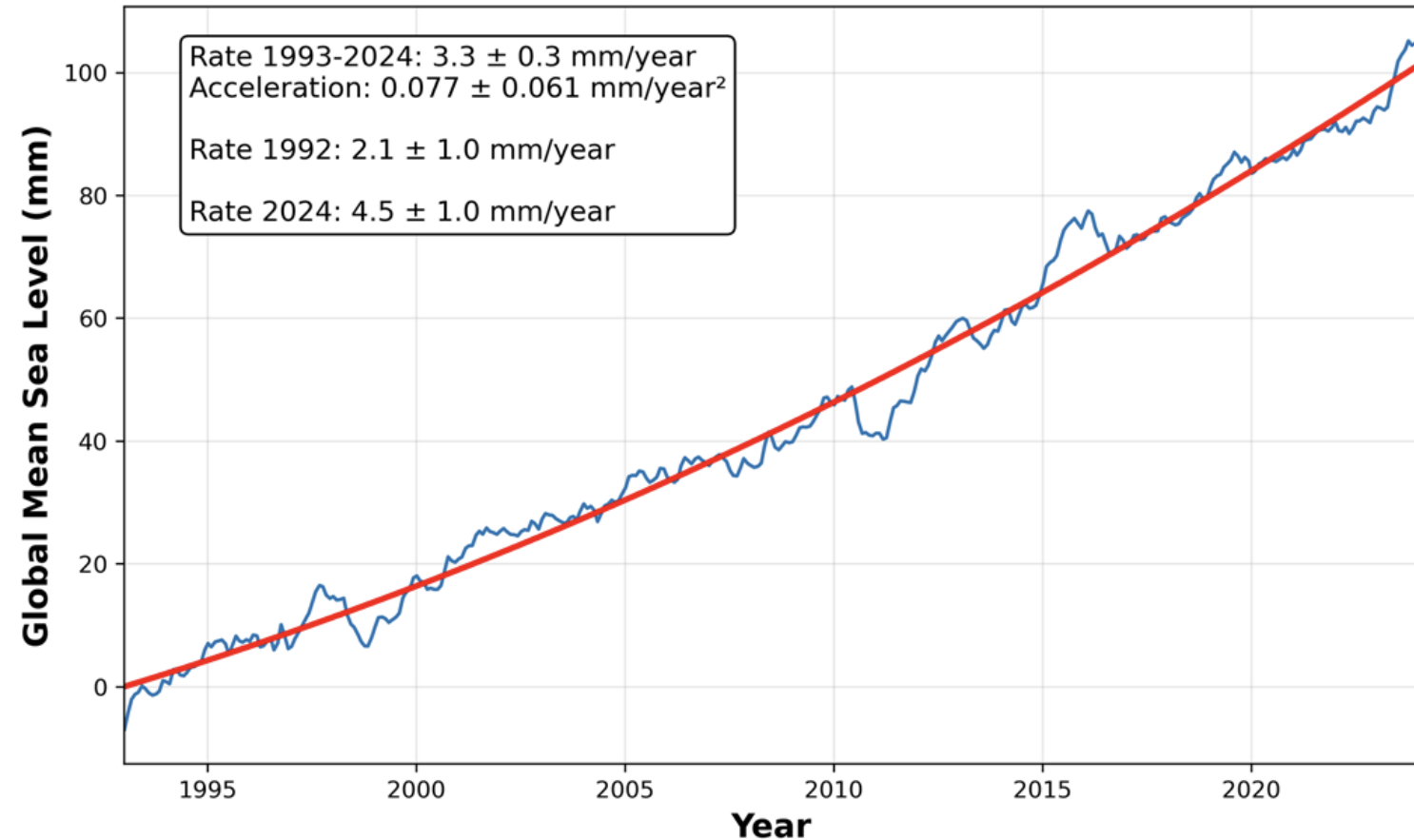
Global mean sea level rose faster in the 20th century than in any prior century over the last three millennia

Fox-Kemper et al. (2021)

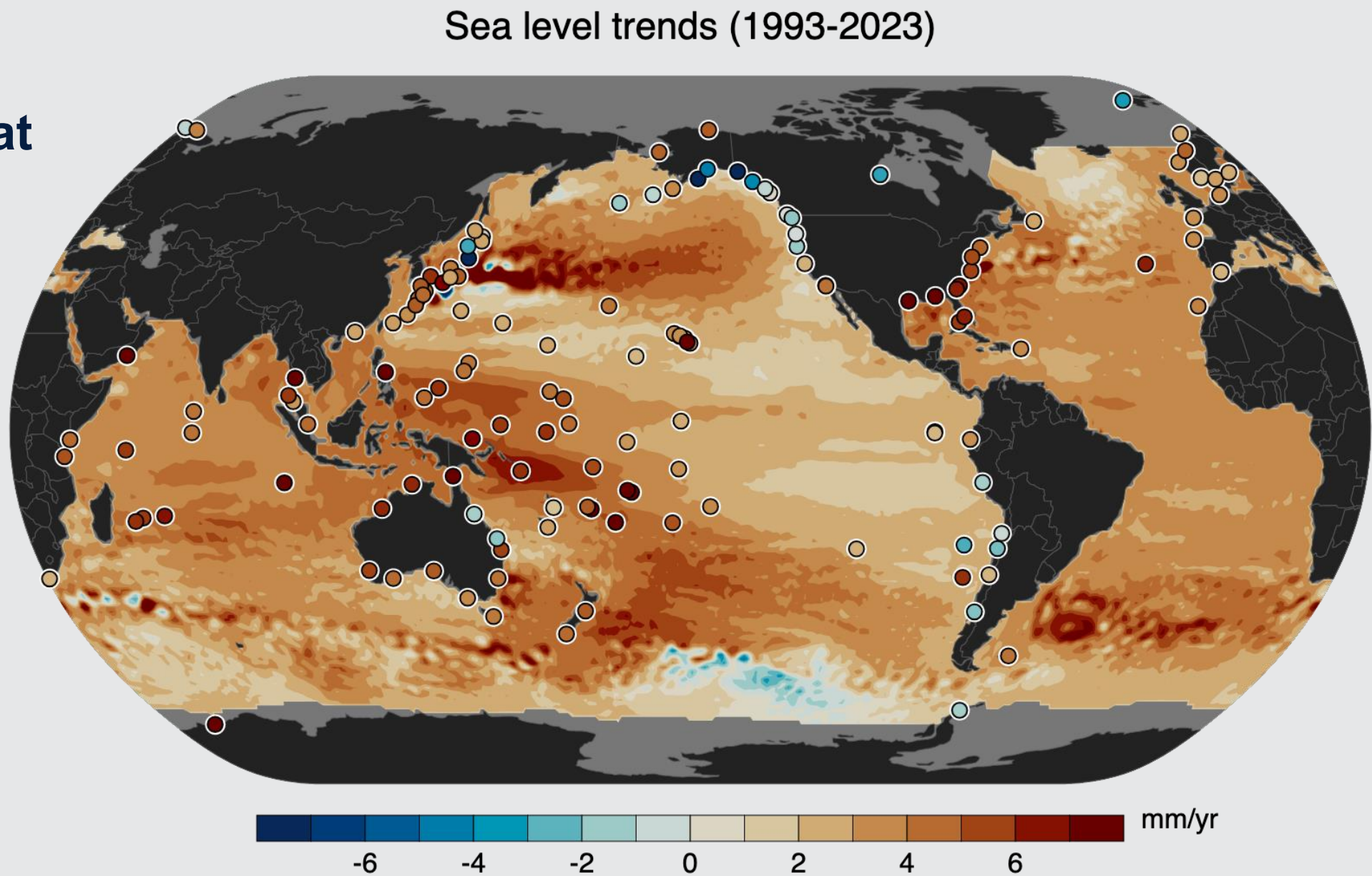


The rate of global sea level rise doubled during the past three decades

Hamlington et al. (2024)



**Sea-level rise
hasn't occurred at
the same rate
everywhere**



High-tide flooding (HTF) rates are increasing

(AKA nuisance flooding, king-tide flooding, tidal flooding, sea-level-rise flooding ...)

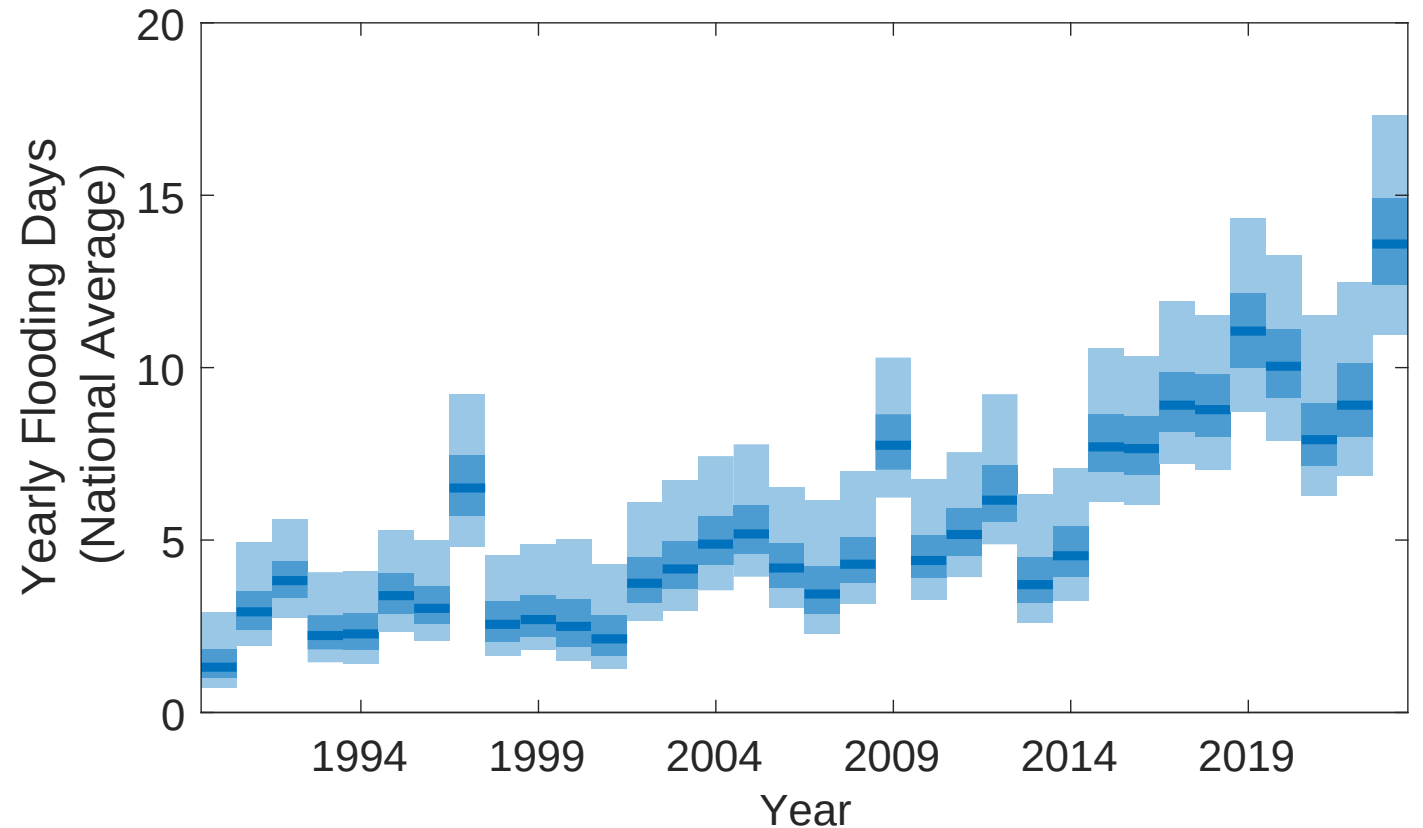
HTF increased by 65% on average globally between 1960-1980 and 1995-2014

Fox-Kemper et al. (2021)

Annual HTF rates in the United States tripled from 1990 to 2020

Sweet et al. (2022)

HTF trends along the United States coastline



How is sea-level changing?

Why is sea-level changing?

And how do we know?

Cautionary note! Terminology ...

- 🤯 🤯 🤯 Sea-level science is a highly interdisciplinary field with **LOTS** of terminology (sterodynamic, manometric, barystatic, geocentric, relative sea level ...) and acronyms (GIA, GRD, GMSL, IB, SSH, VLM ...)
- I won't always try to give exhaustive, technical definitions (but see, for example, Gregory et al. 2019), but rather introduce things as needed
- Don't be stressed! Ask Questions!

**Global sea-level change
is a whole-Earth process**

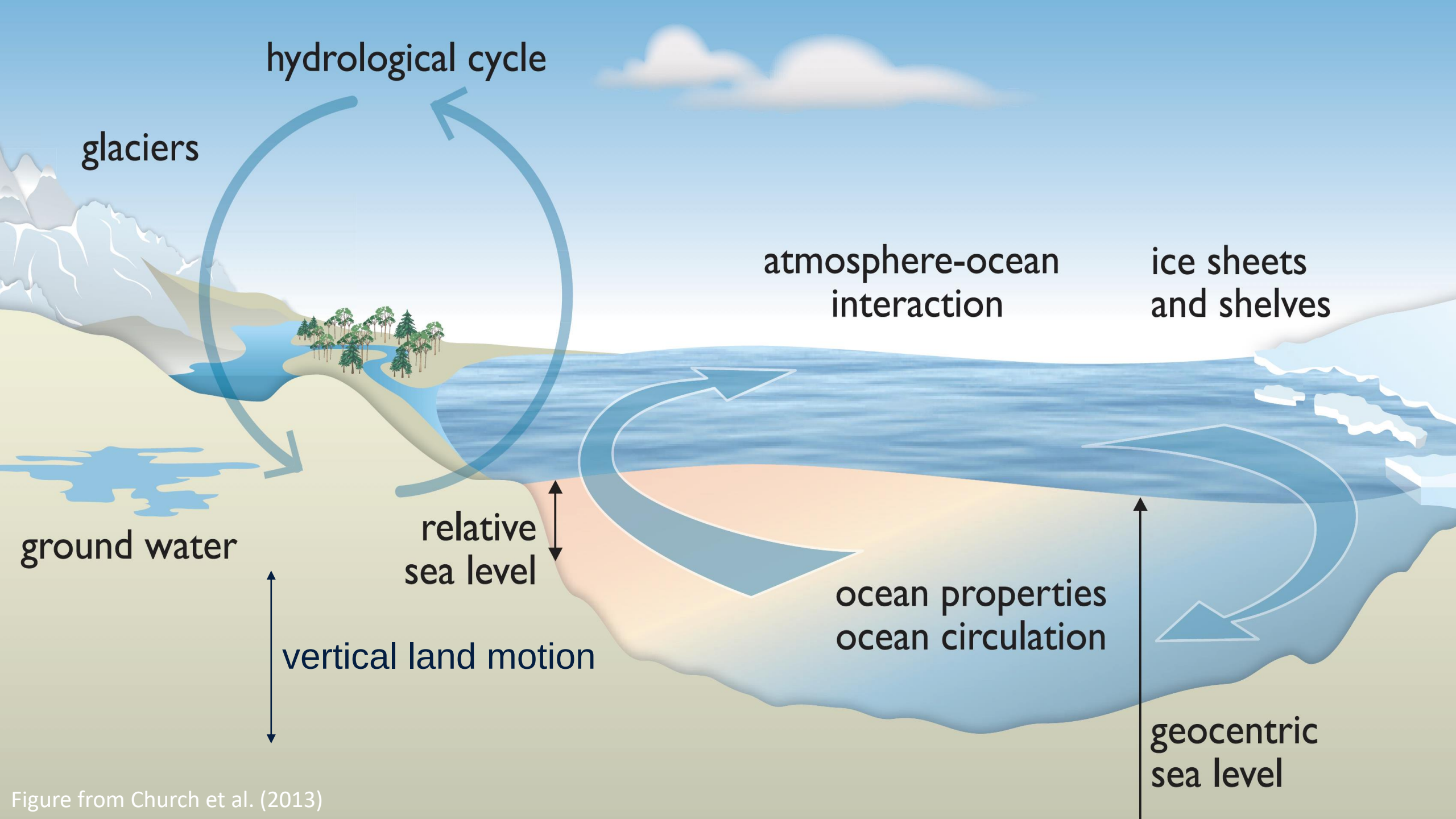
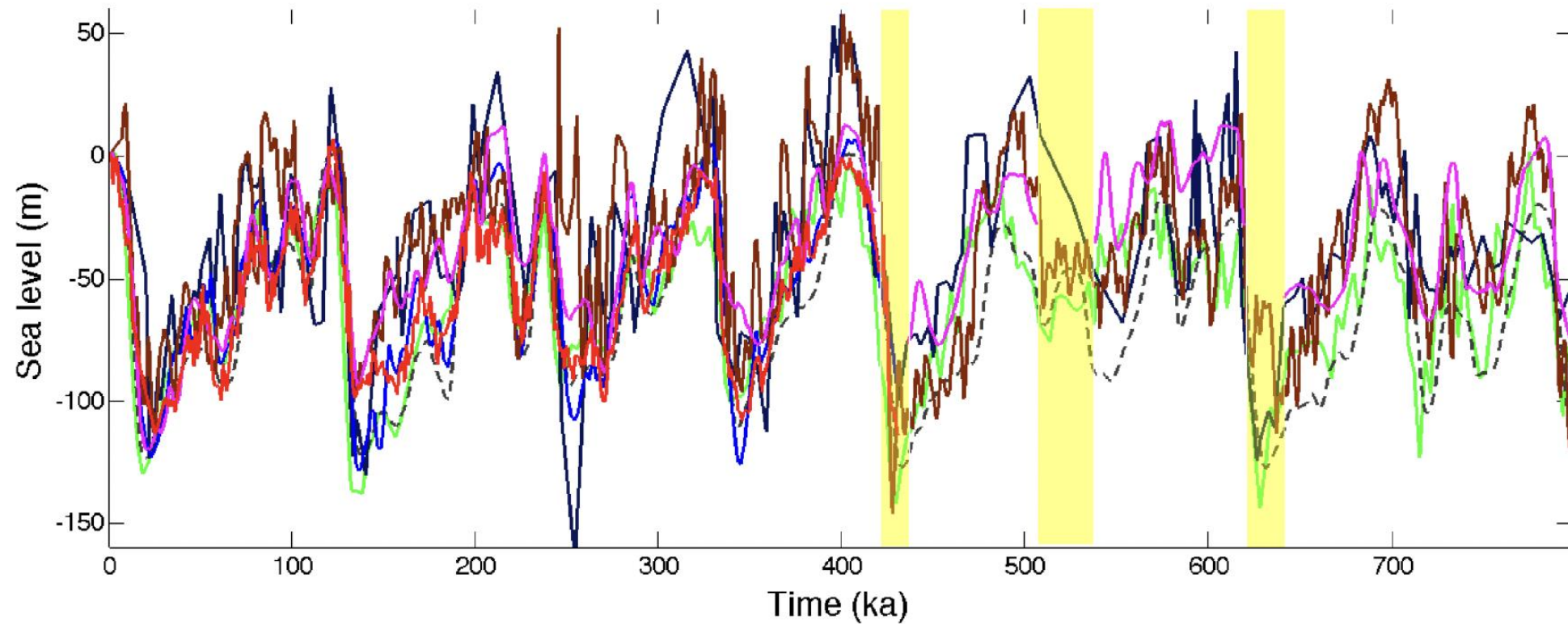


Figure from Church et al. (2013)

Waxing and waning of Pleistocene ice ages



**Sea-level changes are coupled
to ocean circulation & climate**

Sea level strongly constrains Earth's energy imbalance and hydrological cycle

Start with hydrostatic balance

$$\frac{dp}{dz} = -\rho g$$

with hydrostatic pressure p , vertical coordinate z , density ρ , gravity g .

- Integrate from seafloor H to (geocentric) sea level ζ and rearrange

$$\zeta = \frac{p_b - p_s}{\rho_s g} + \left(-\frac{1}{\rho_s g} \int_{-H}^0 \rho \, dz \right)$$

where p_b / p_s are bottom/surface pressure and ρ_s is surface density.

Sea level strongly constrains Earth's energy imbalance and hydrological cycle

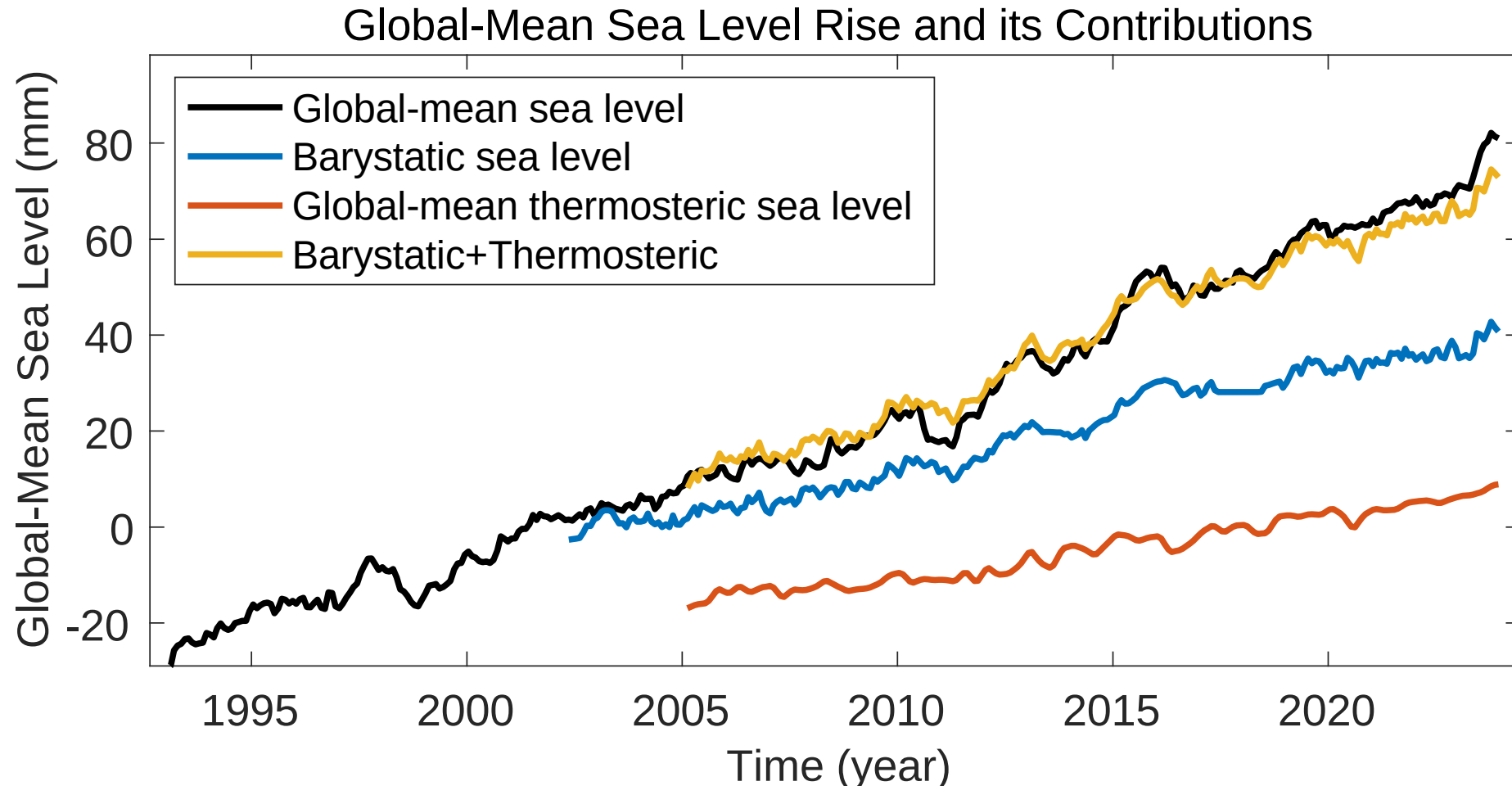
- Geocentric sea-level changes arise from contributions from changes in ocean mass and ocean density
- **Steric sea-level changes** ζ_ρ arise from changes in ocean density at constant mass

$$\zeta_\rho = -\frac{1}{\rho_s g} \int_{-H}^0 \rho \, dz$$

- **Manometric sea-level changes** ζ_m come from changes in the local mass of the ocean per unit area at constant density

$$\zeta_m = \frac{p_b - p_s}{\rho_s g}$$

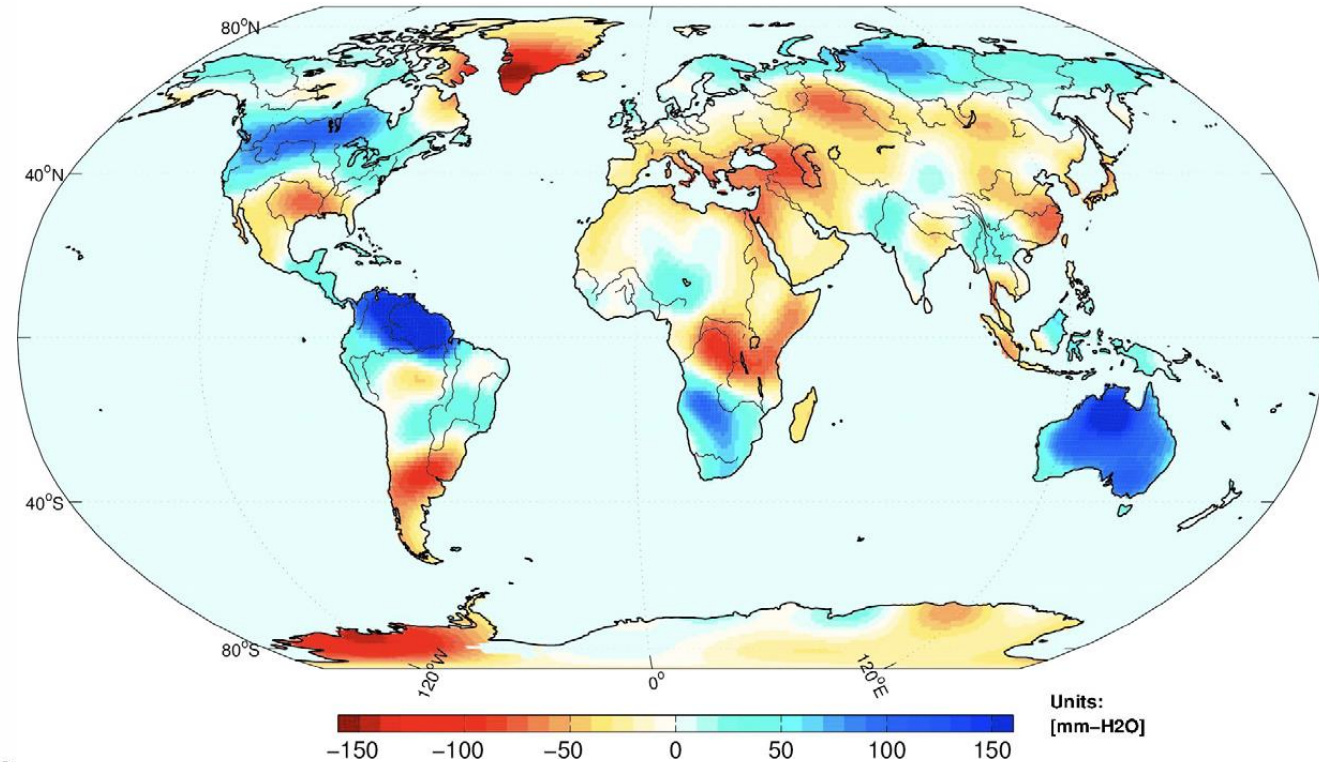
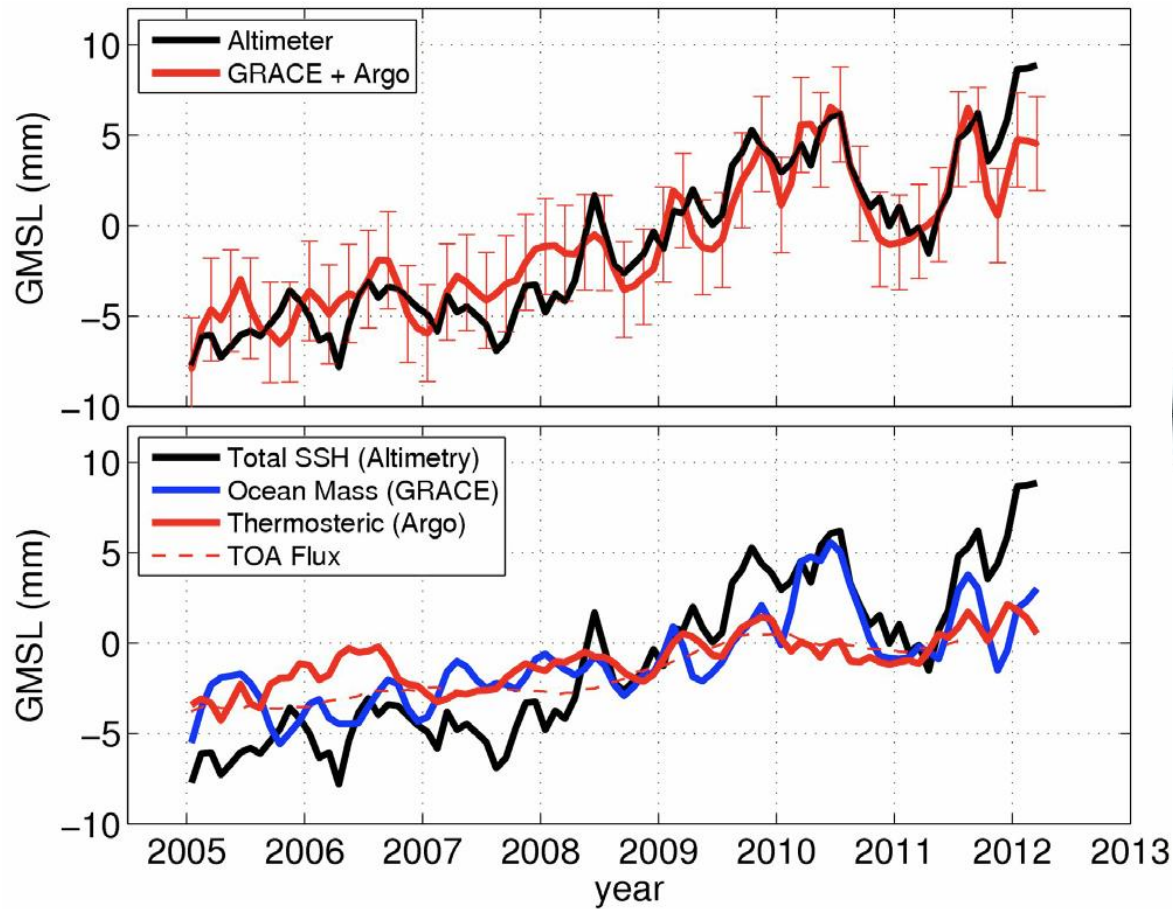
Sea level strongly constrains Earth's energy imbalance and hydrological cycle



 **Barystatic sea level** is the global average of manometric sea level 

Data from Beckley et al. (2017), Wiese et al. (2022), Roemmich and Gilson (2009)

Sea level strongly constrains Earth's energy imbalance and hydrological cycle



Sea level is coupled to the general circulation

- Consider the forced, linear shallow-water equations (e.g., Gill, 1982)

$$\frac{\partial \zeta}{\partial t} + \frac{\partial}{\partial x} (Hu) + \frac{\partial}{\partial y} (Hv) = \frac{P - E}{\rho}$$

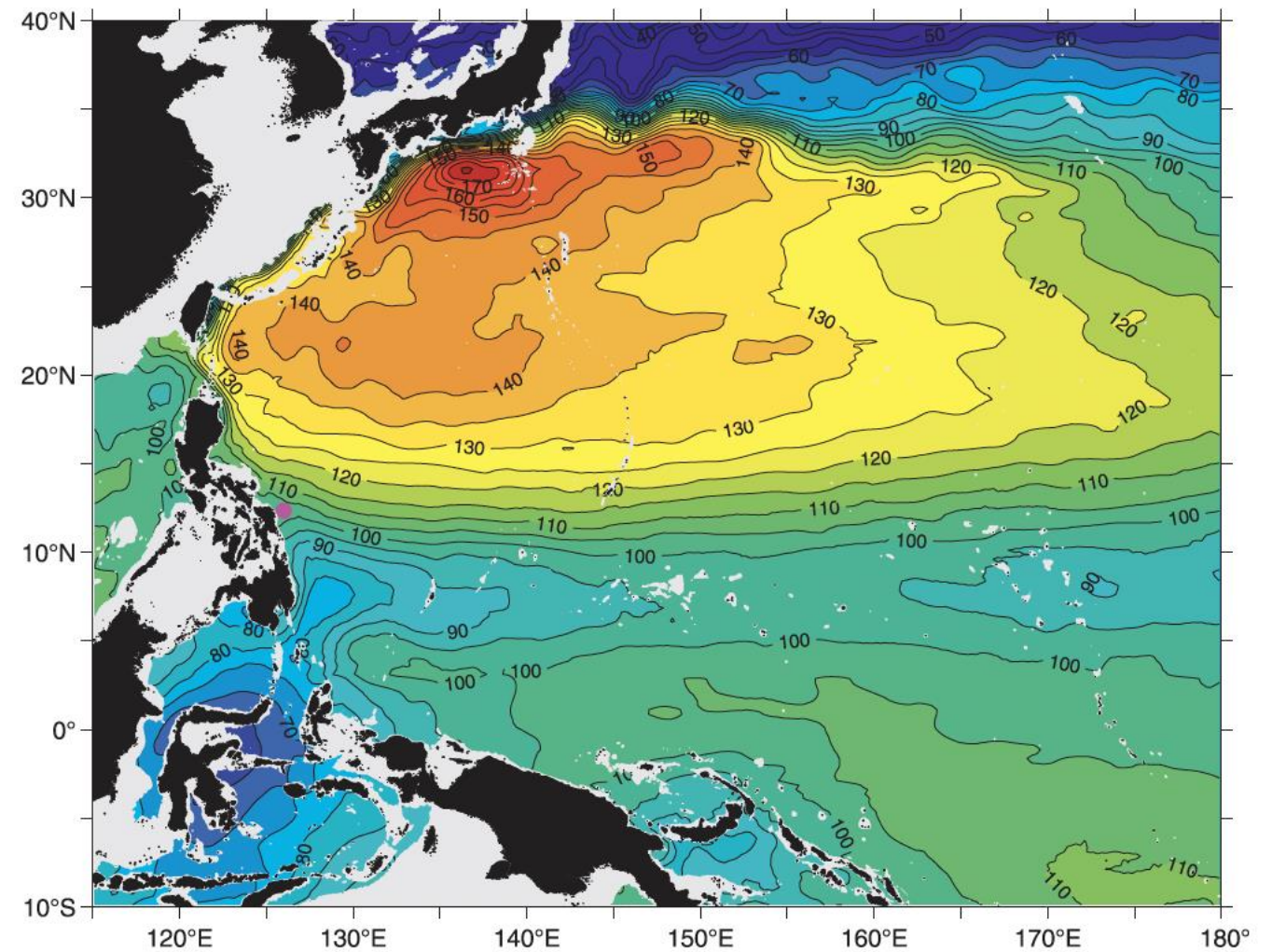
$$\frac{\partial u}{\partial t} - fv = -g \frac{\partial}{\partial x} \left(\zeta + \frac{p_s}{\rho g} \right) + \frac{X_s - X_b}{\rho H}$$

$$\frac{\partial v}{\partial t} + fu = -g \frac{\partial}{\partial y} \left(\zeta + \frac{p_s}{\rho g} \right) + \frac{Y_s - Y_b}{\rho H}$$

u/v horizontal velocities, f Coriolis, P/E precipitation/evaporation, X_s , X_b , Y_s , Y_b horizontal surface and bottom stresses

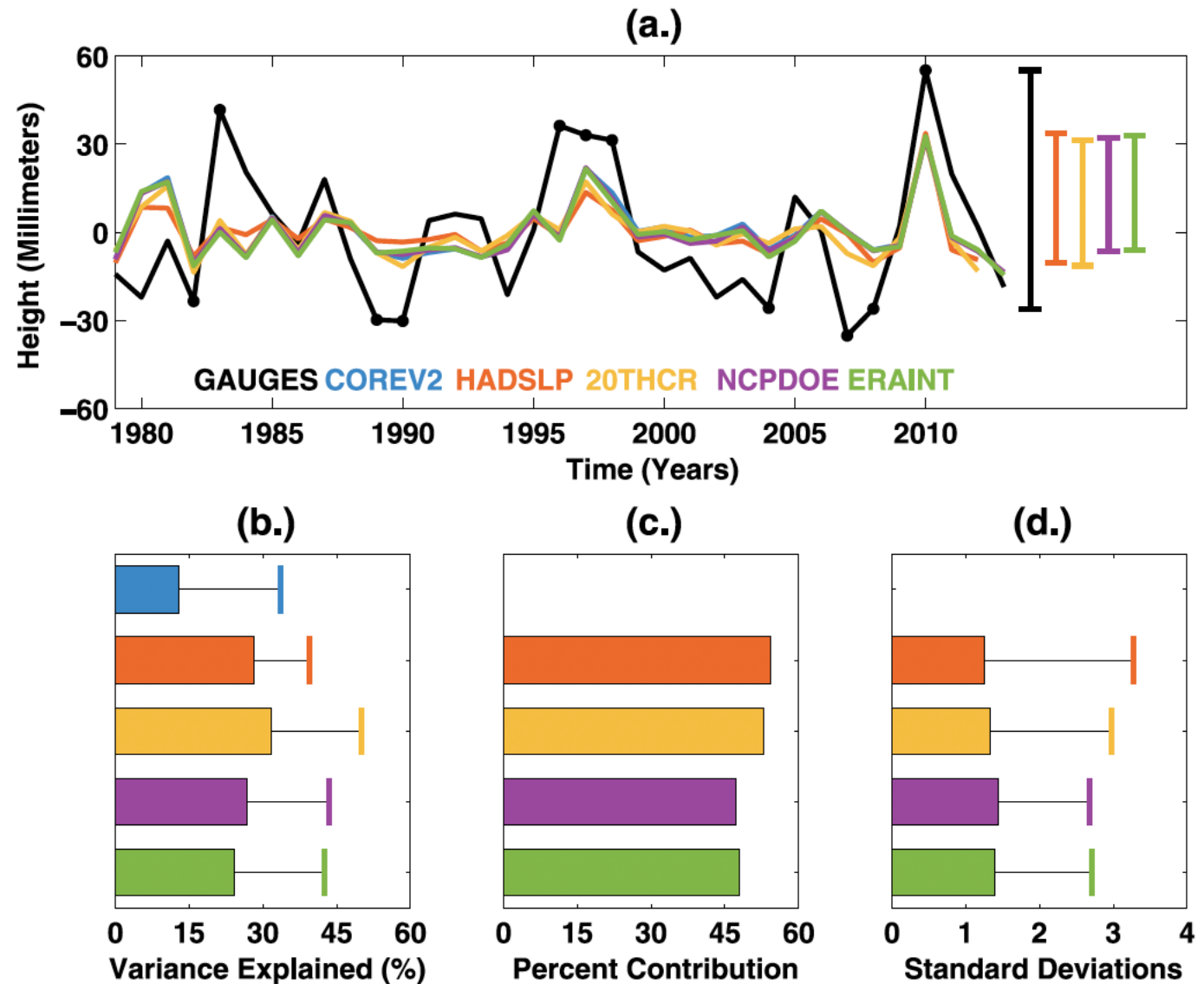
Simplified physics: geostrophic balance

Time-independent, unforced,
frictionless limit of the shallow
water equations



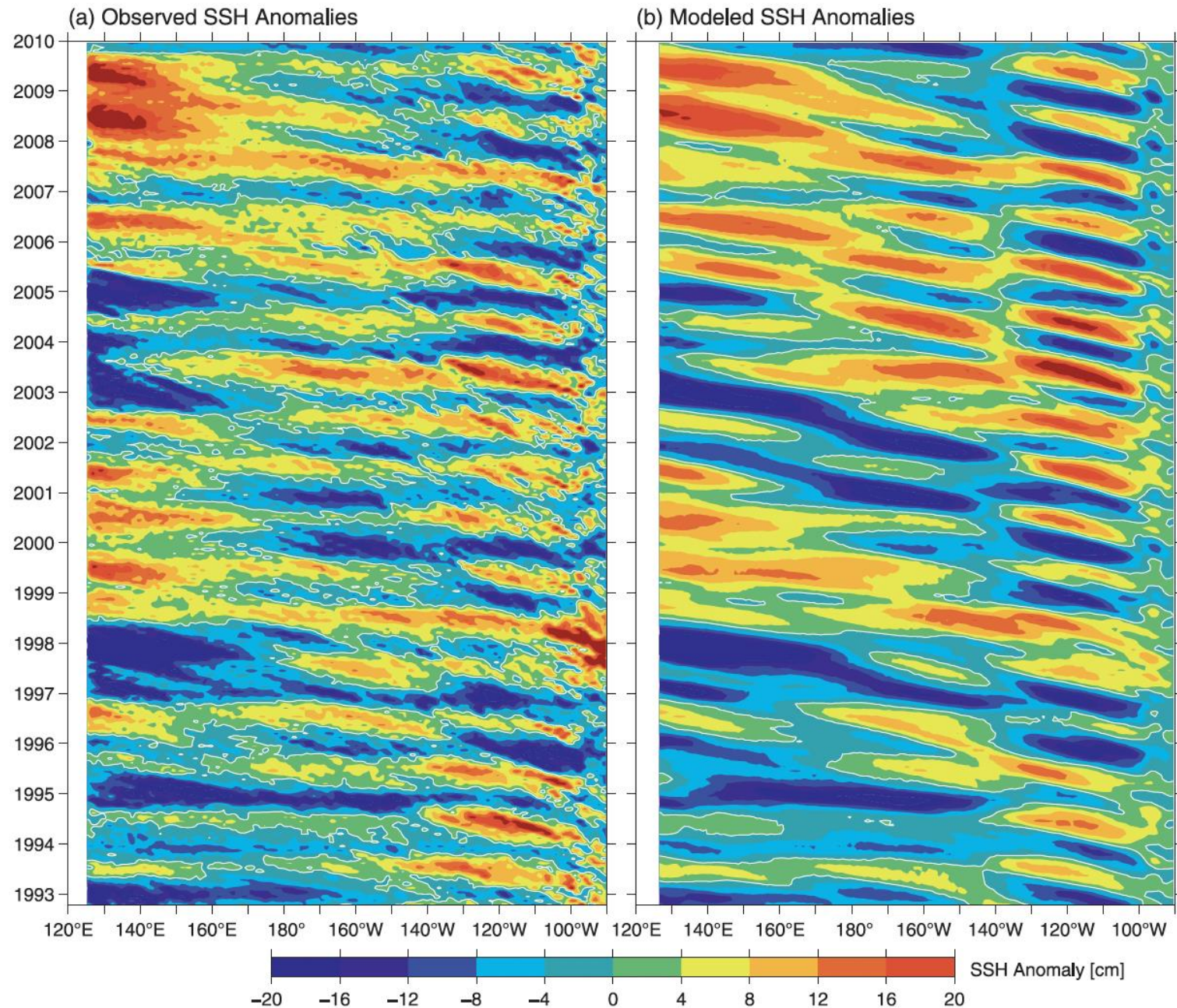
Simplified physics: inverted barometer

Time-independent, frictionless,
static, pressure-forced limit of the
shallow water equations



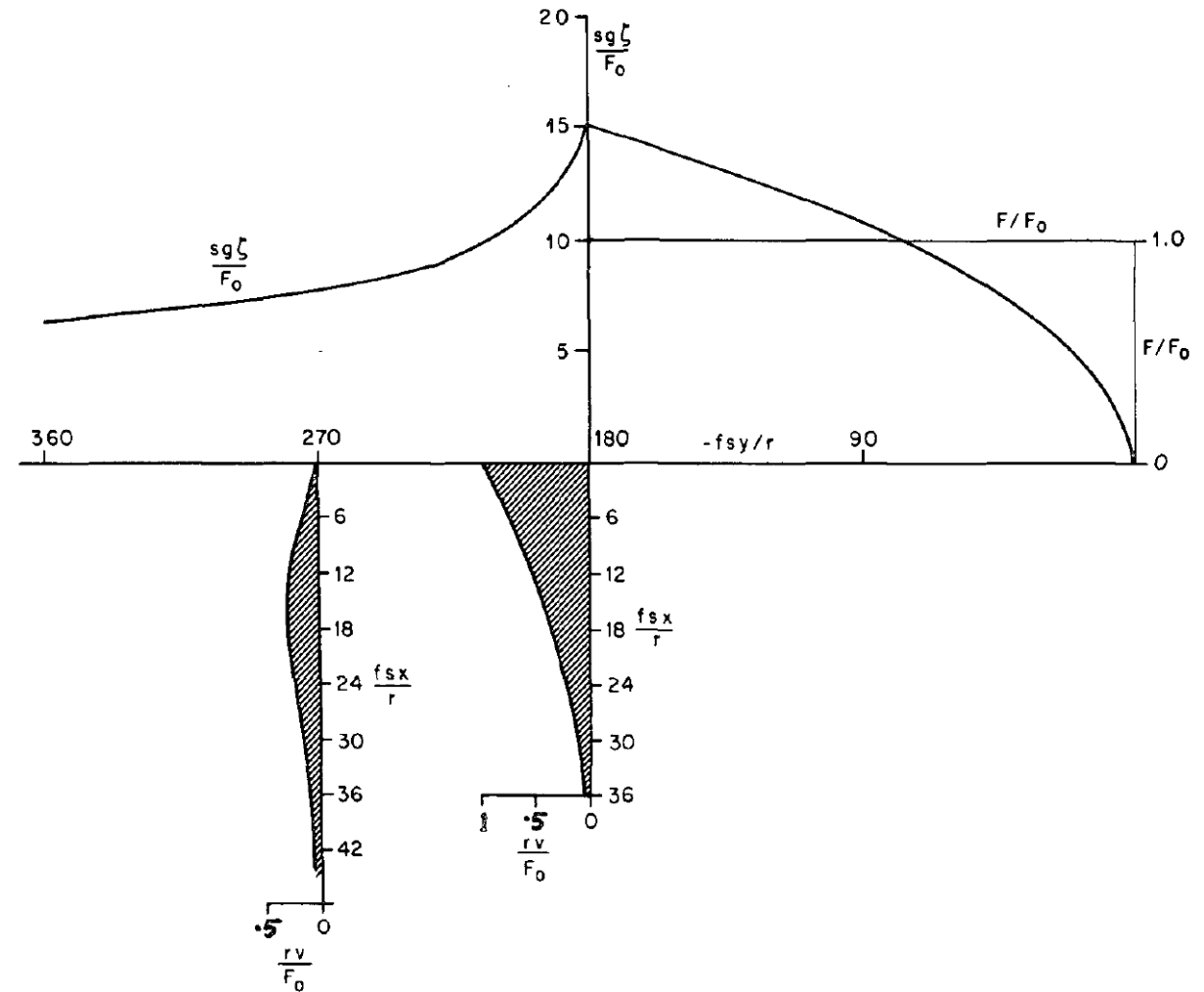
Simplified physics: damped wind-driven long Rossby waves

Large-scale, sub-inertial limited
of the shallow water equations
forced by surface wind stress



Simplified physics: arrested topographic wave (& generalizations)

Time independent with variable
bottom bathymetry (different
varieties with different forcing)

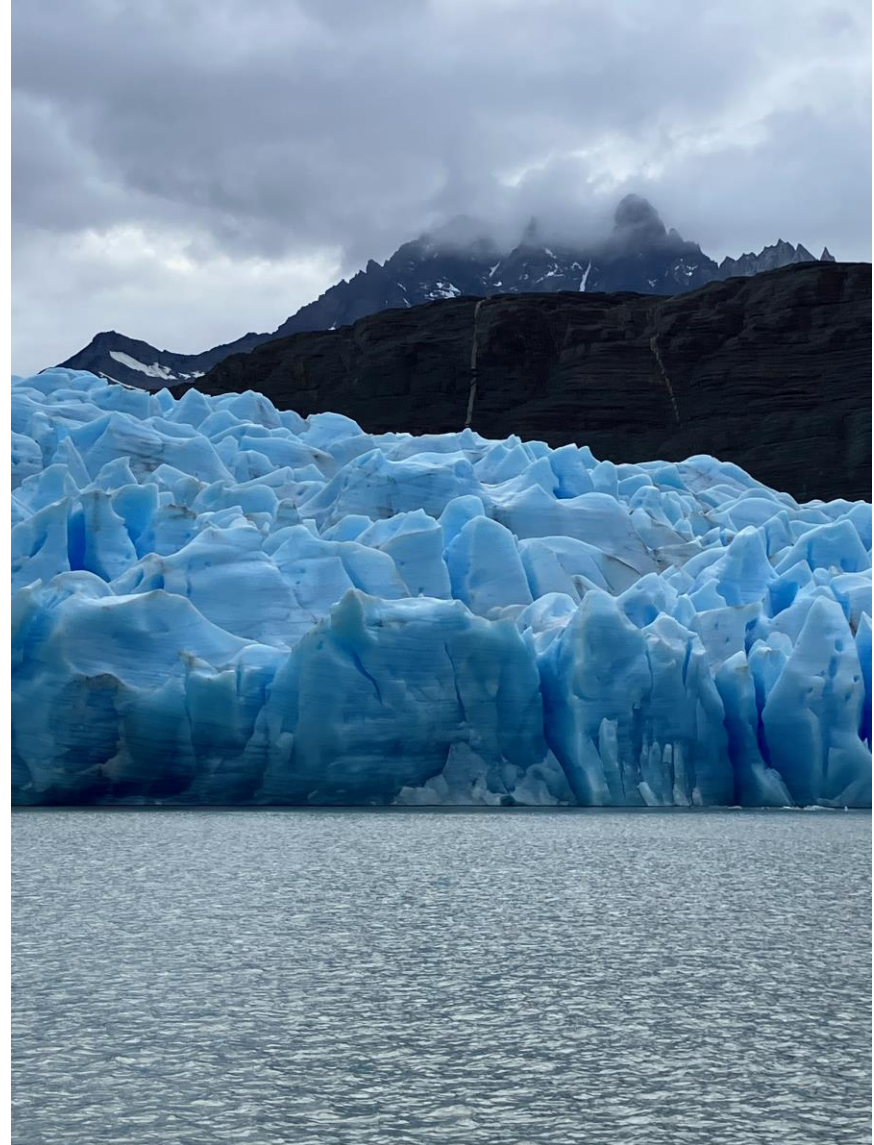


Sea level is coupled to the general circulation

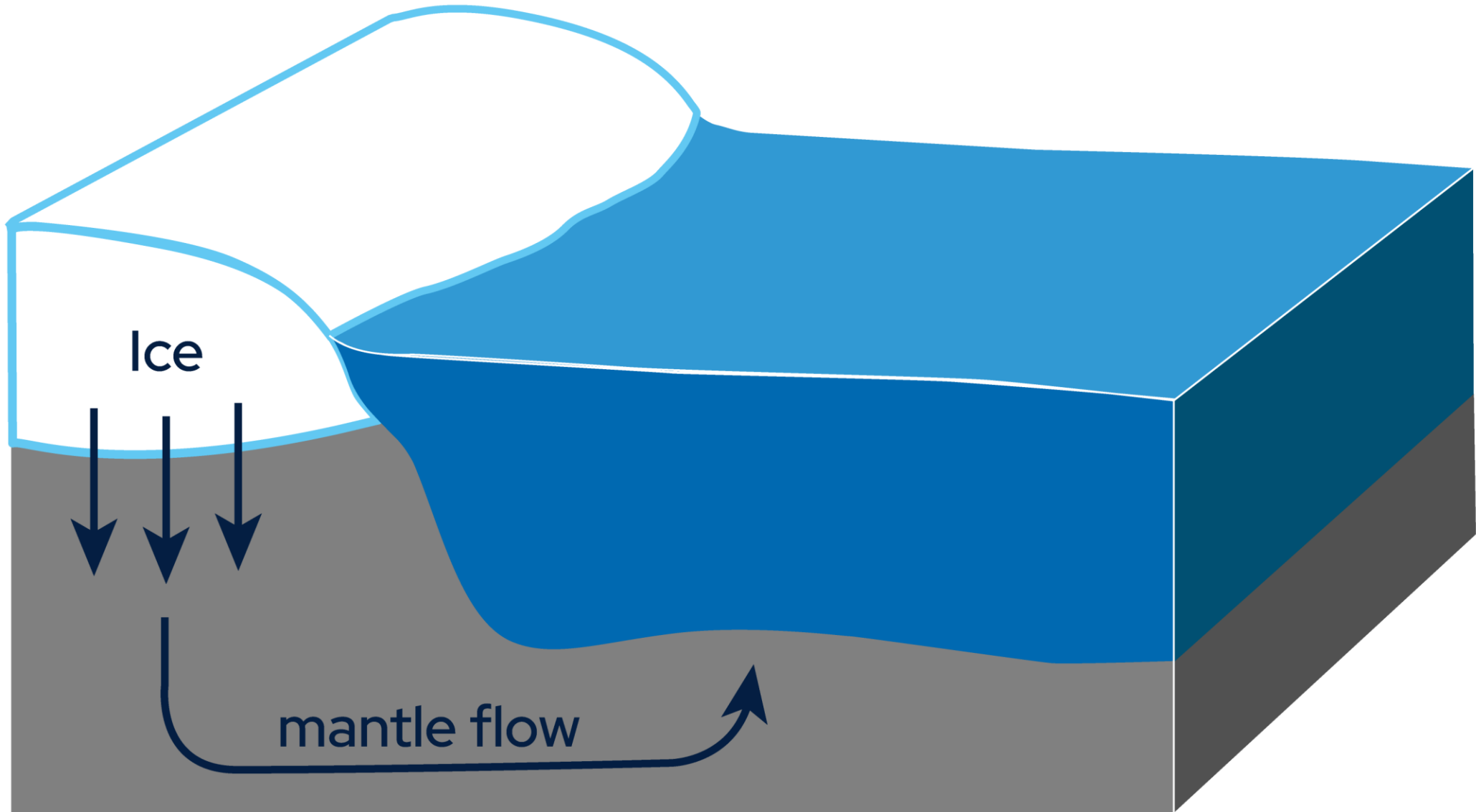
- This was only the briefest possible overview of the coupling between coastal and open-ocean sea level with circulation!
- I passed over many other processes and forcing mechanisms!
 - Other wave motions (coastal and equatorial Kelvin waves, topographic Rossby waves, continental-shelf waves, coastal-trapped waves ...)
 - High-frequency phenomena (tsunamis and meteotsunamis, surface gravity waves, tides, storm surge ...)
 - Dynamic response to barometric pressure
 - Near-, mid-, and far-field response to river discharge
 - Forcing by large-scale evaporation and precipitation
 - Sea-level changes that arise from changing surface heat flux
 - Relation to large-scale features like gyres and overturning

Gravity, rotation, and deformation (GRD)

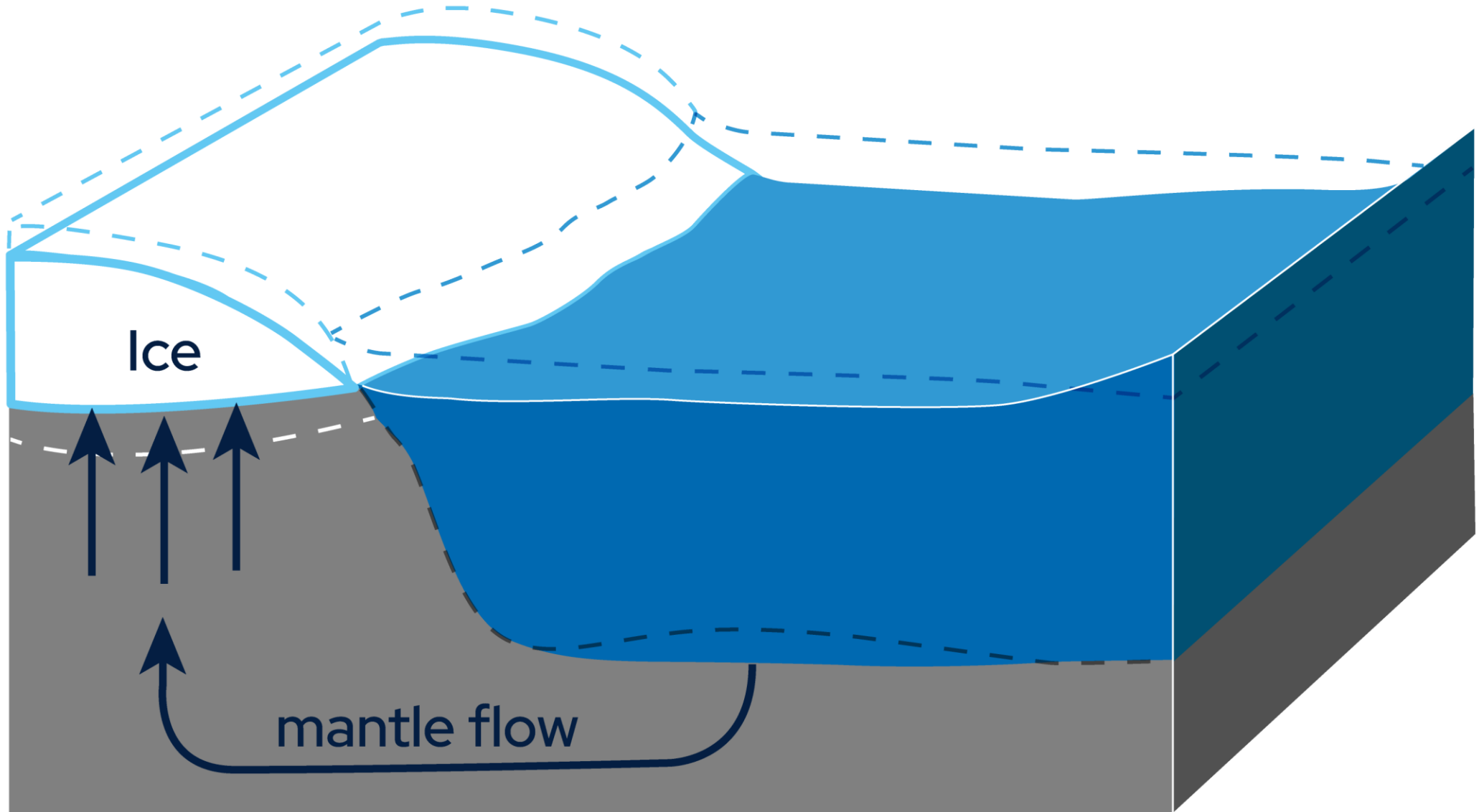
- I've assumed Earth's solid surface, gravity field, and rotation vector are time-invariant ... which isn't true!
- These things also matter for sea level (e.g., distinction between *geocentric* sea level and *relative* sea level)



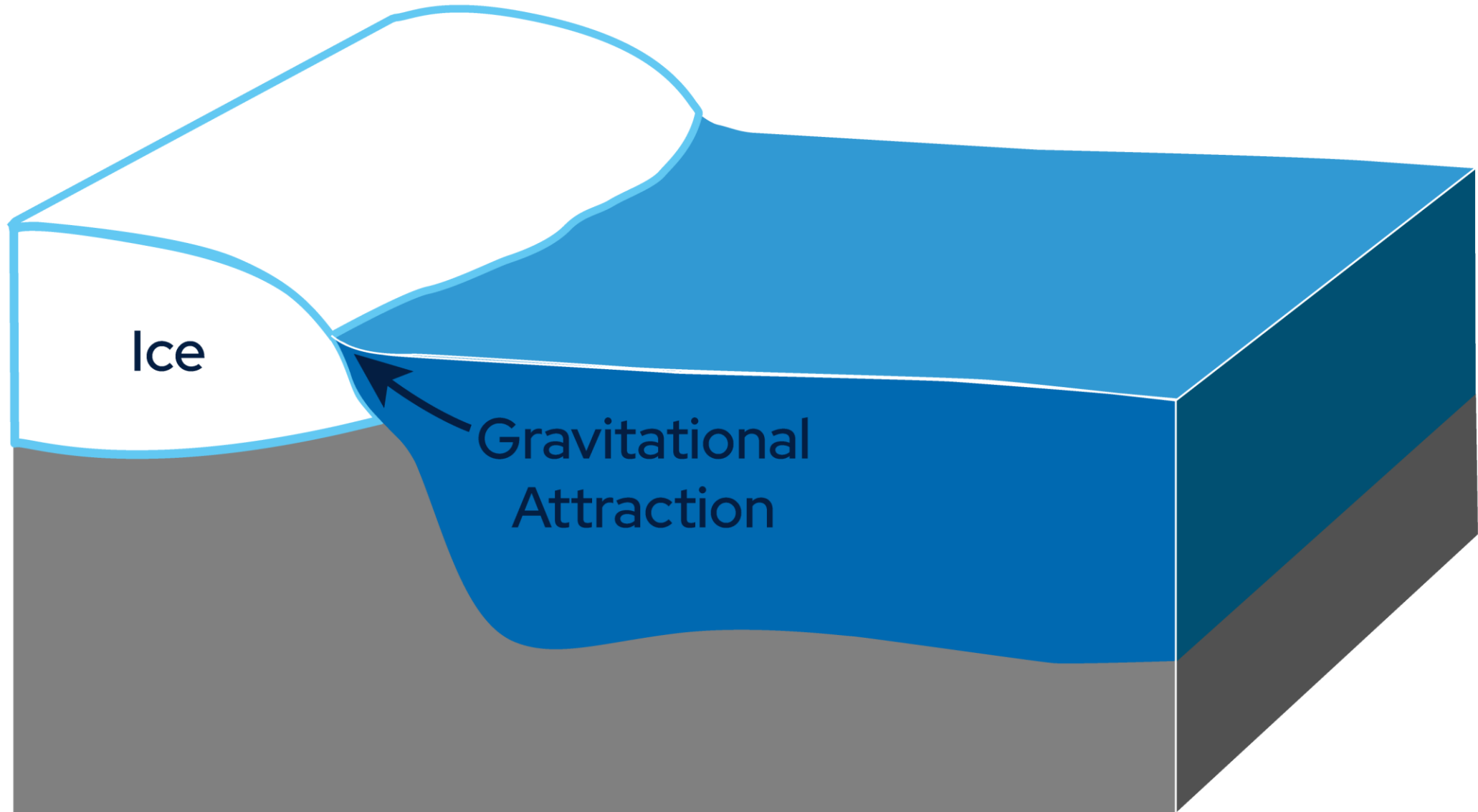
Gravity, rotation, and deformation



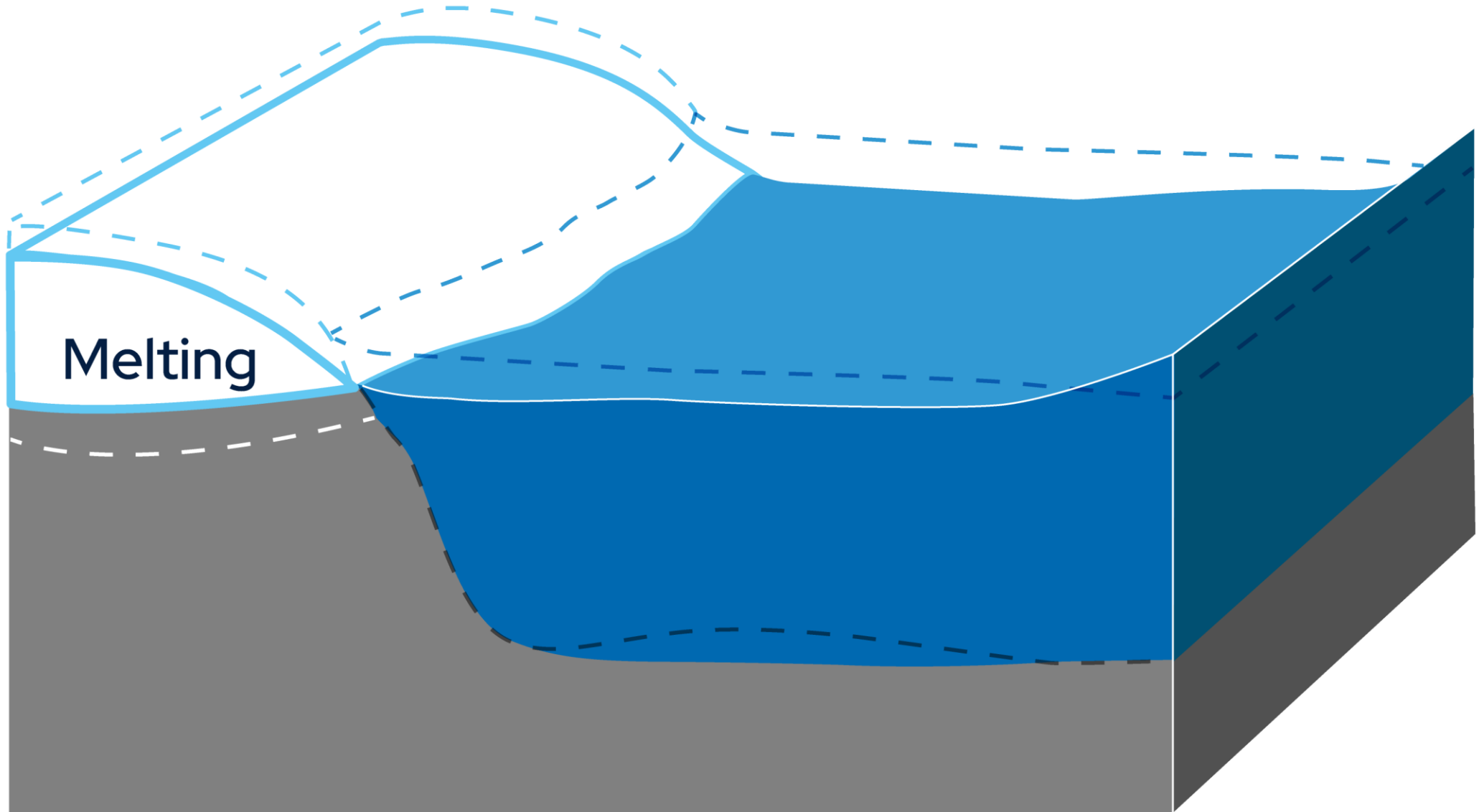
Gravity, rotation, and deformation



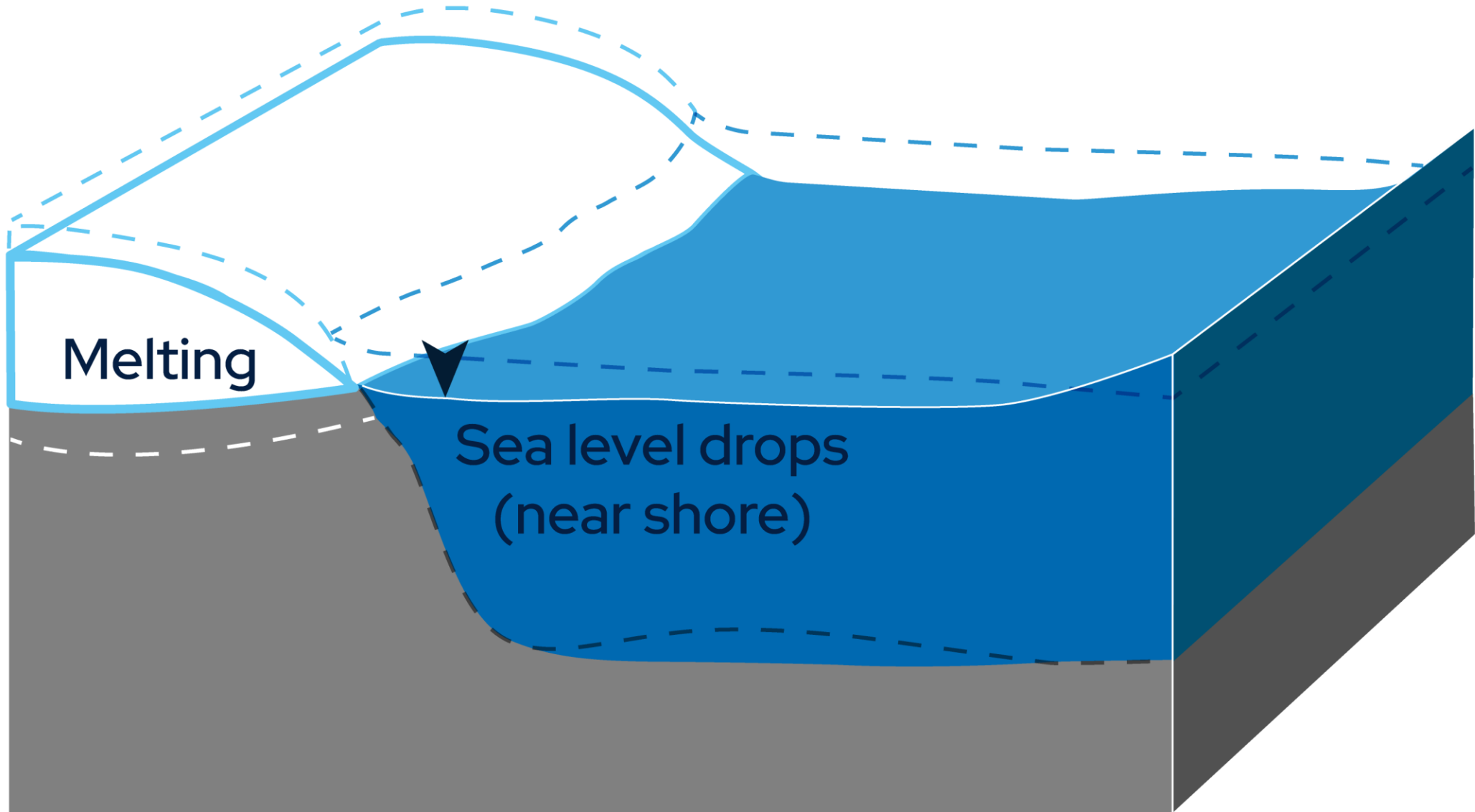
Gravity, rotation, and deformation



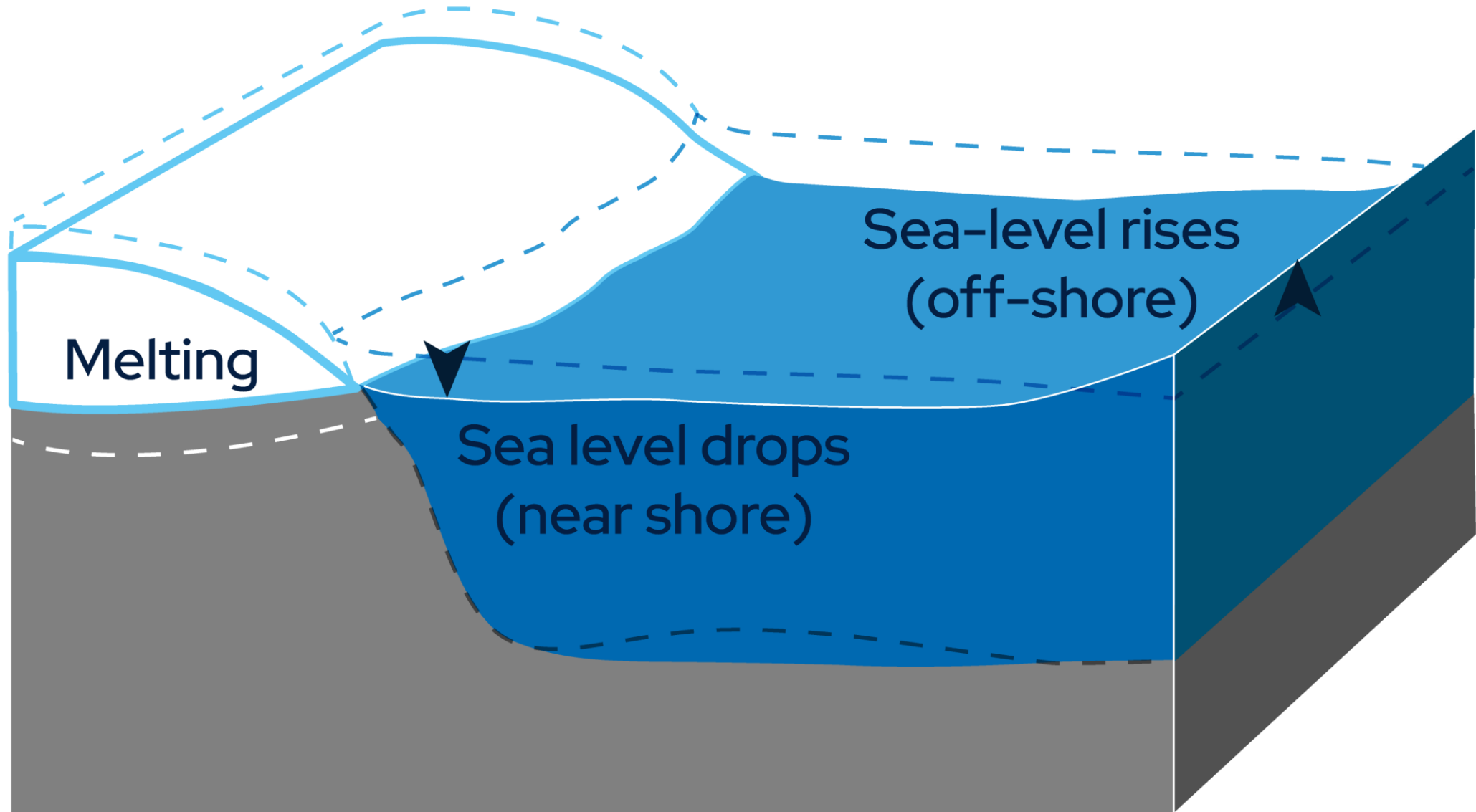
Gravity, rotation, and deformation



Gravity, rotation, and deformation



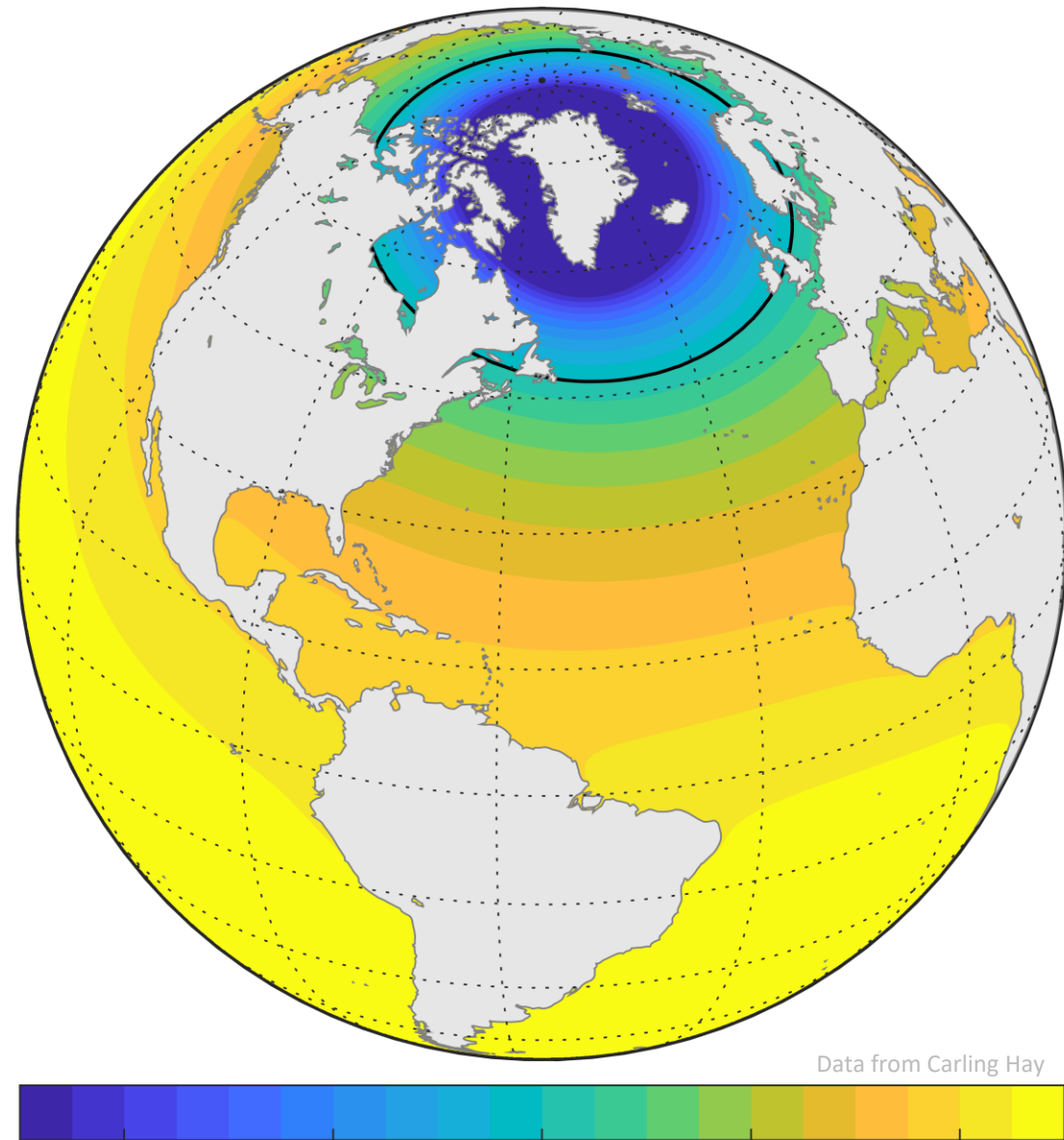
Gravity, rotation, and deformation



Gravity, rotation, and deformation

Elastic sea-level “fingerprint” of
Greenland Ice Sheet melt

Data courtesy of Carling Hay



← Fall

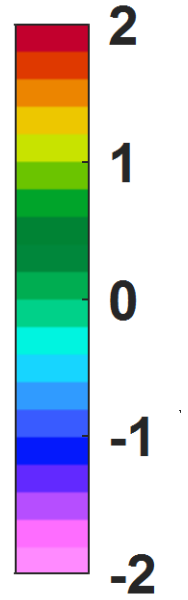
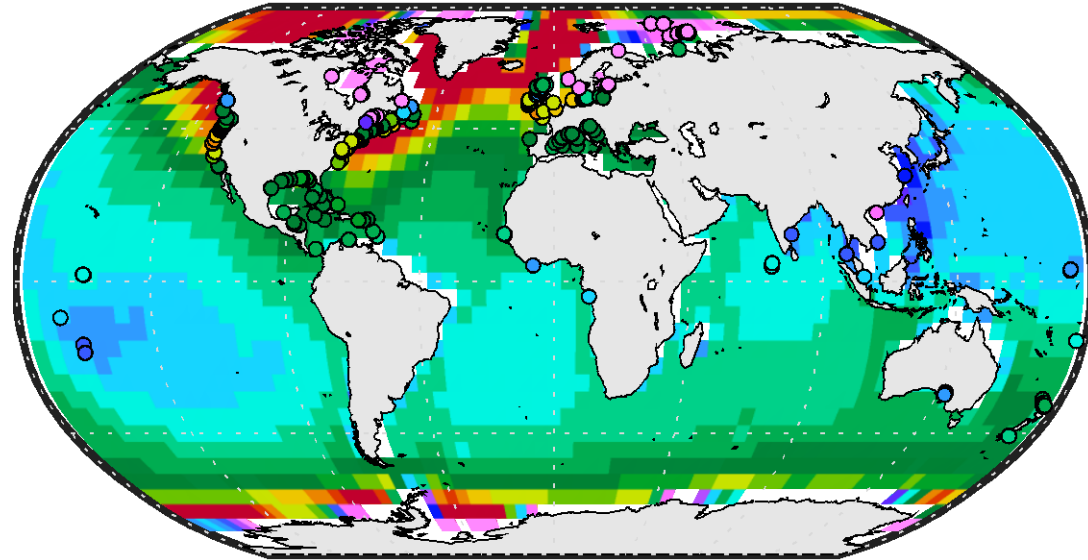
Rise →

Gravity, rotation, and deformation

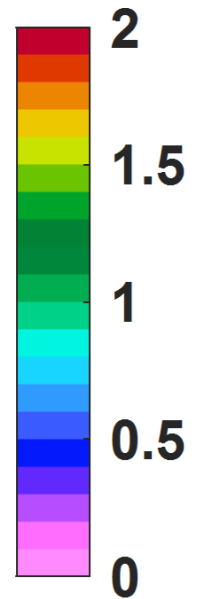
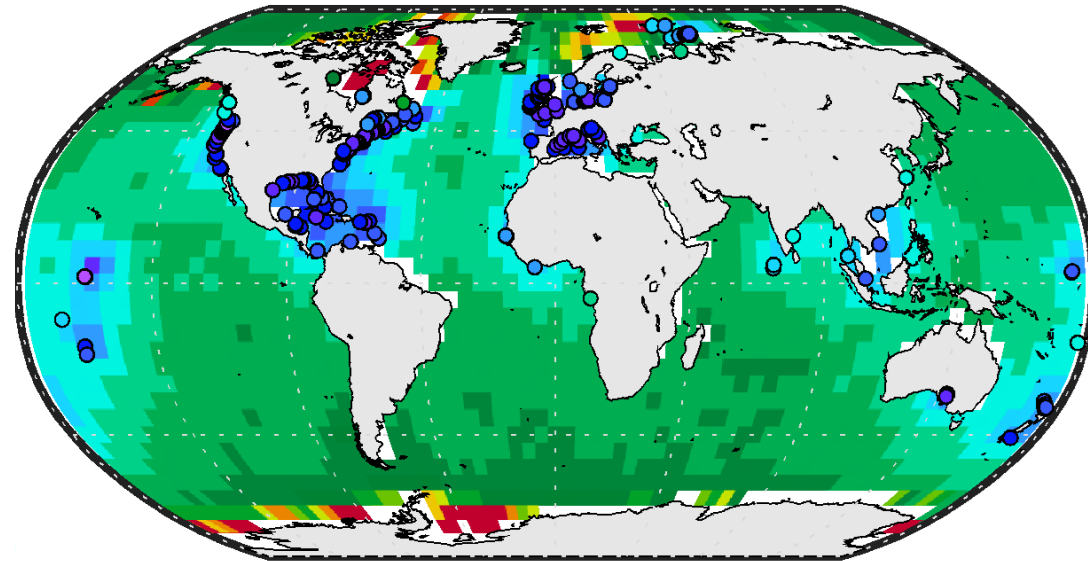
Probabilistic estimate of relative sea-level trends during the past 2,000 years

(Piecuch et al., in prep)

Best Estimate (mm/yr)

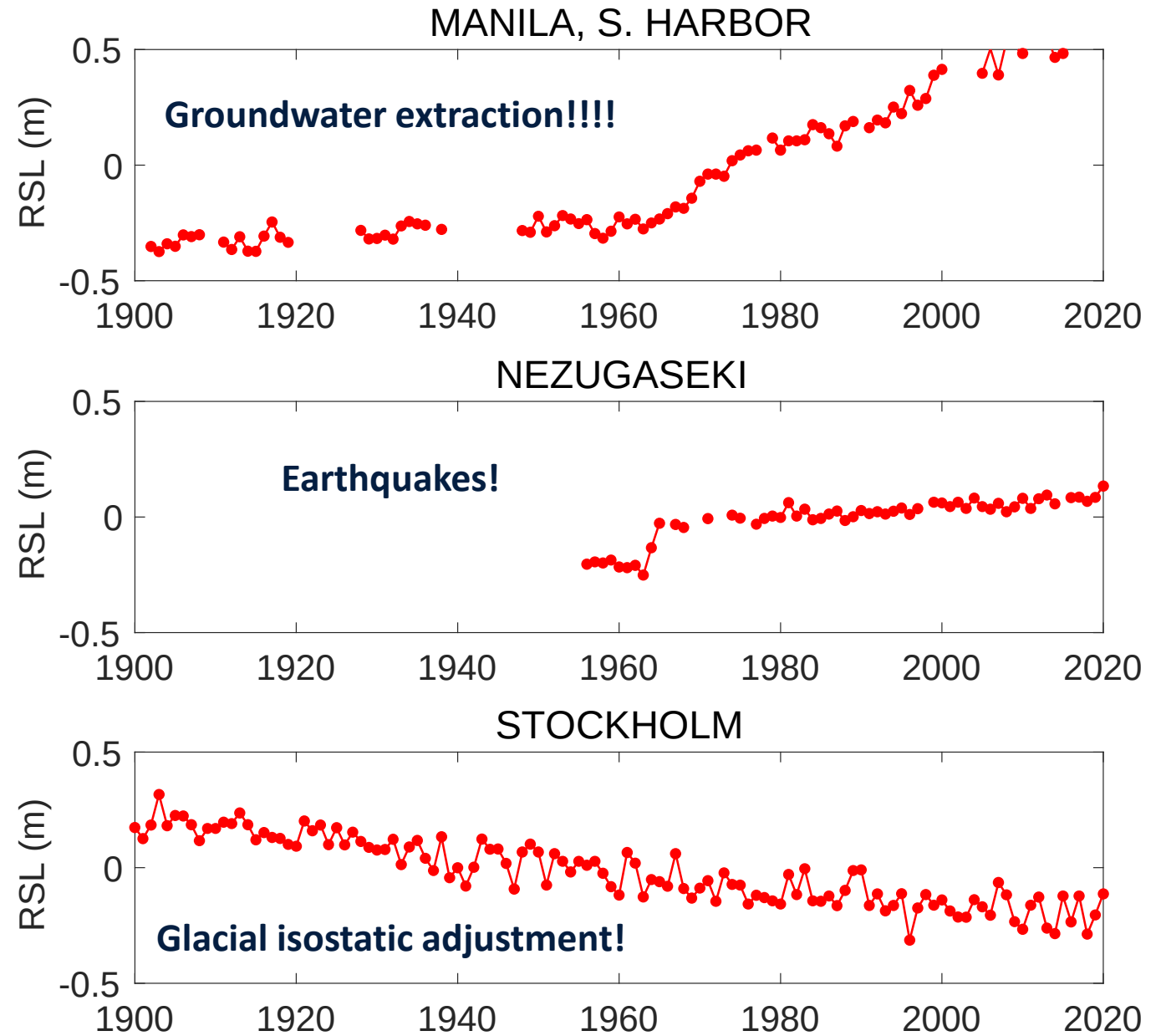


Standard Deviation(mm/yr)



Gravity, rotation, and deformation

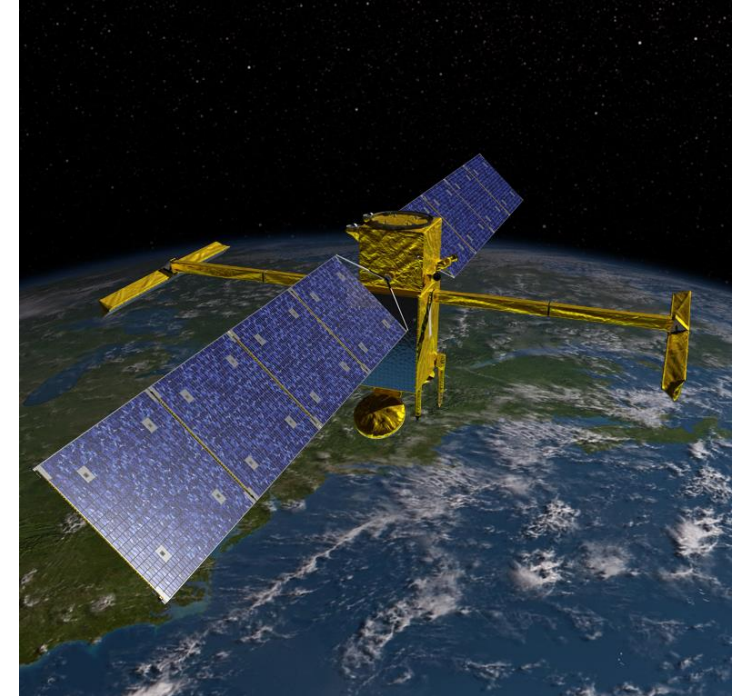
Example tide-gauge records
(Holgate et al., 2013)



**NASA data and models have greatly advanced
understanding of sea level**

NASA altimetry observations

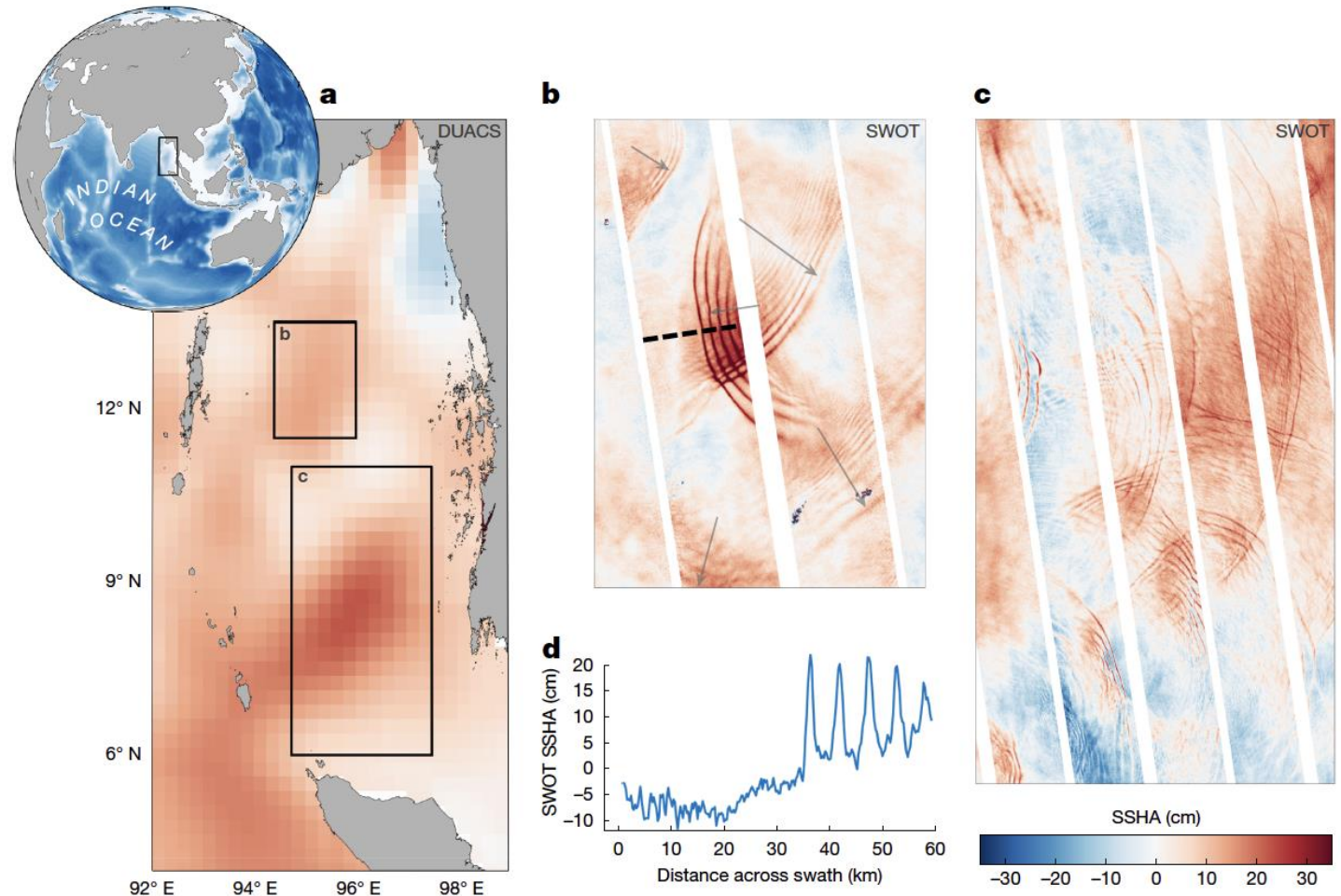
TOPEX/Poseidon, Jason series, Sentinel-6/MF, SWOT ...



Artists' renditions courtesy of NASA

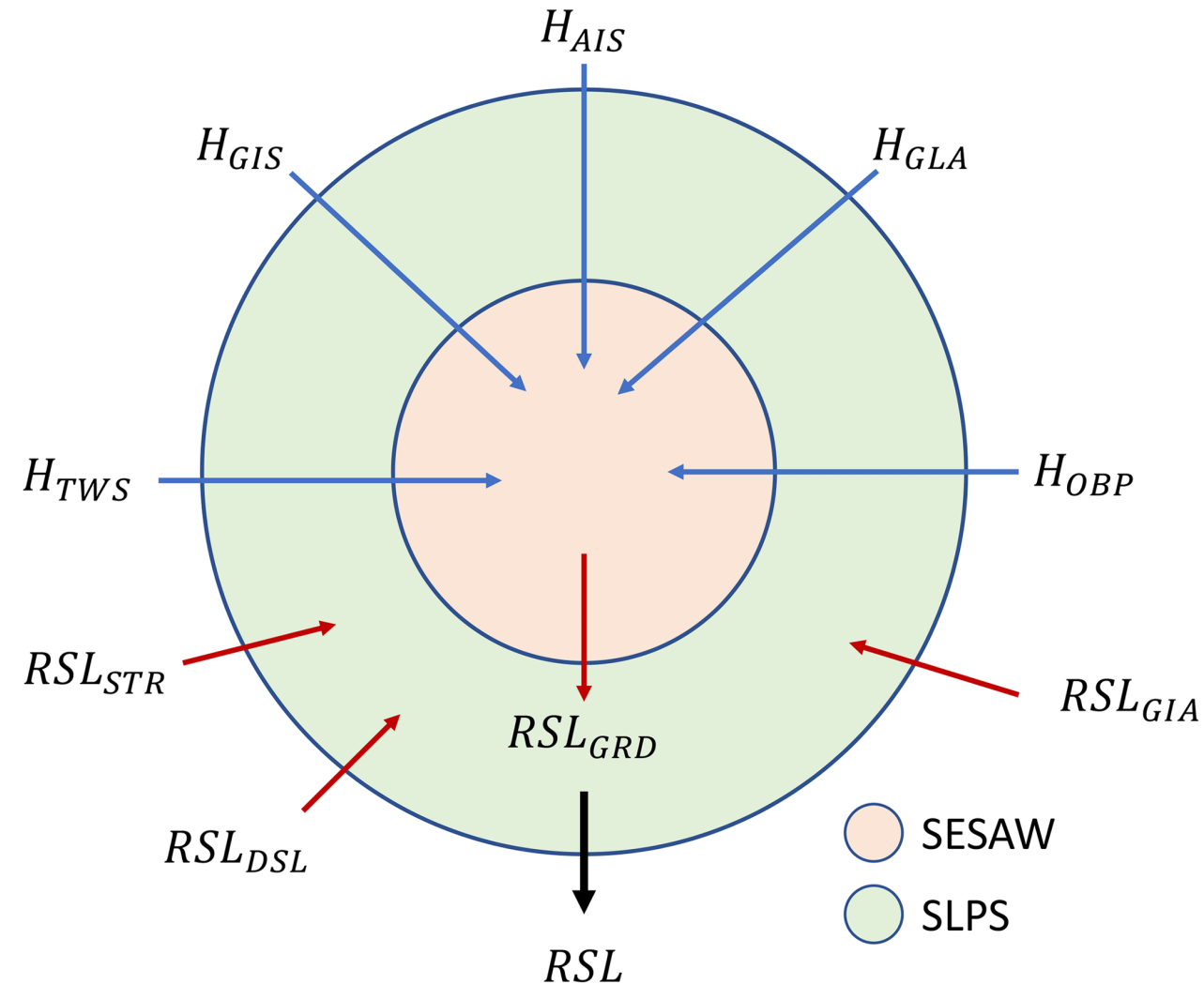
NASA altimetry observations

TOPEX/Poseidon, Jason series,
Sentinel-6/MF, SWOT ...



(mostly) NASA observations (and models)

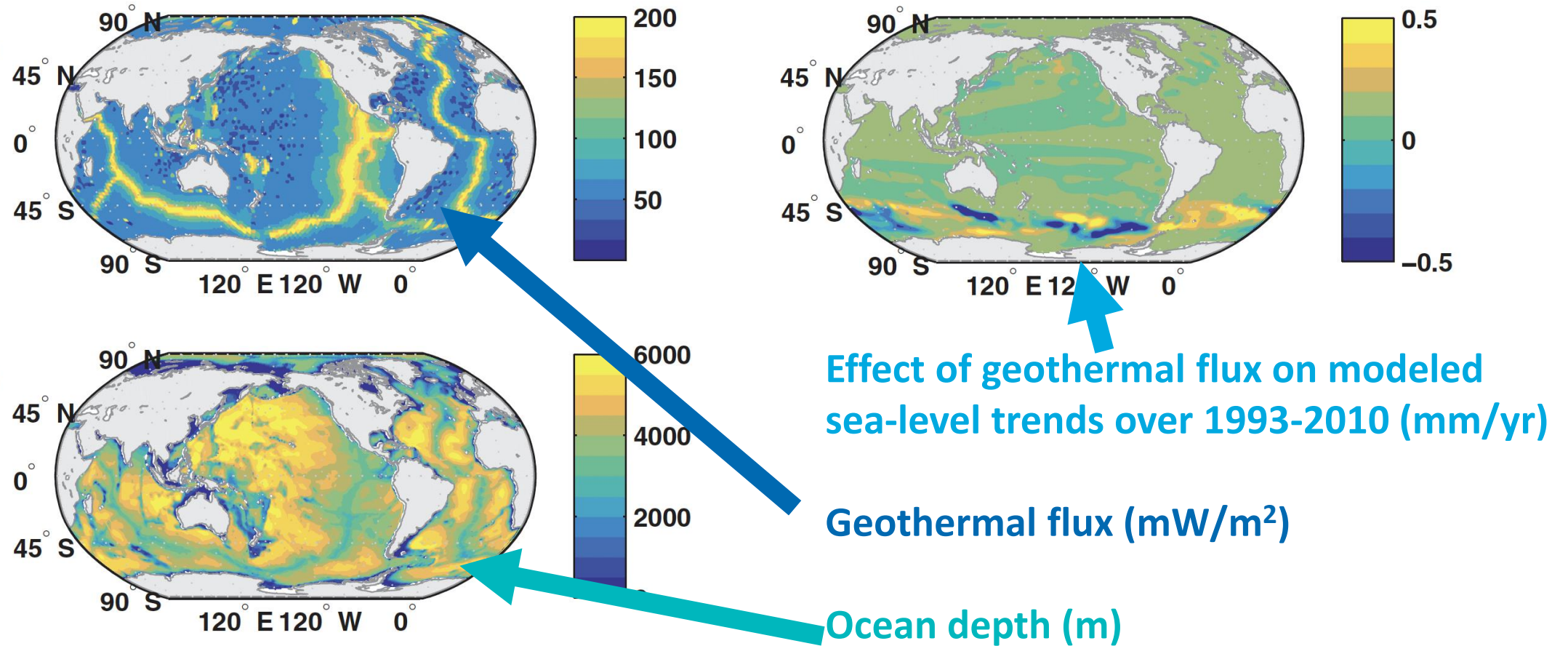
- ICESat-2
- Sentinel-3
- Cryosat-2
- GRACE & GRACE-FO
- InSAR
- GNSS
- 🧐🧐🧐 ECCO 🧐🧐🧐
- GISS ModelE
- ISSM-SLPS
- ... and more!



**ECCO is a powerful tool for quantifying ocean
contributions to sea-level change**

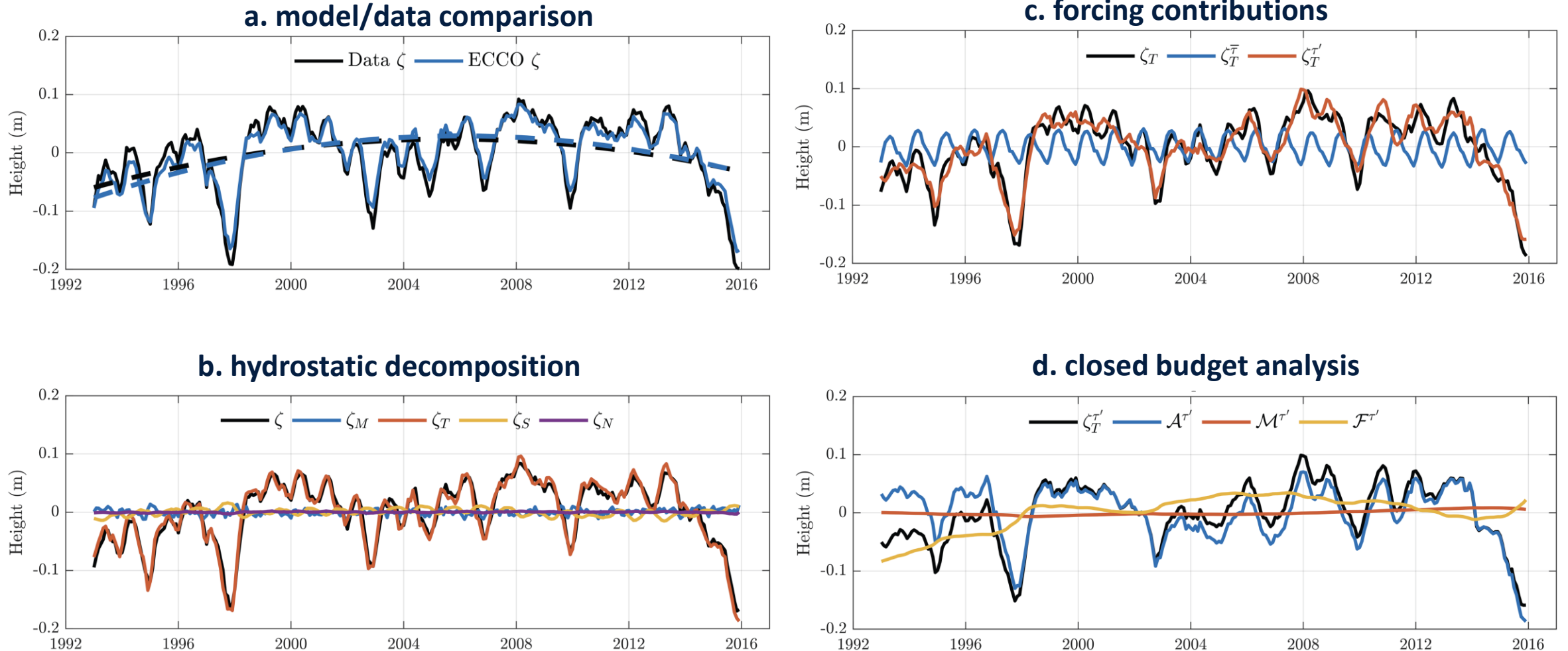
ECCO vignettes: forcing perturbation experiments

What influence does a geothermal flux bottom boundary condition have?



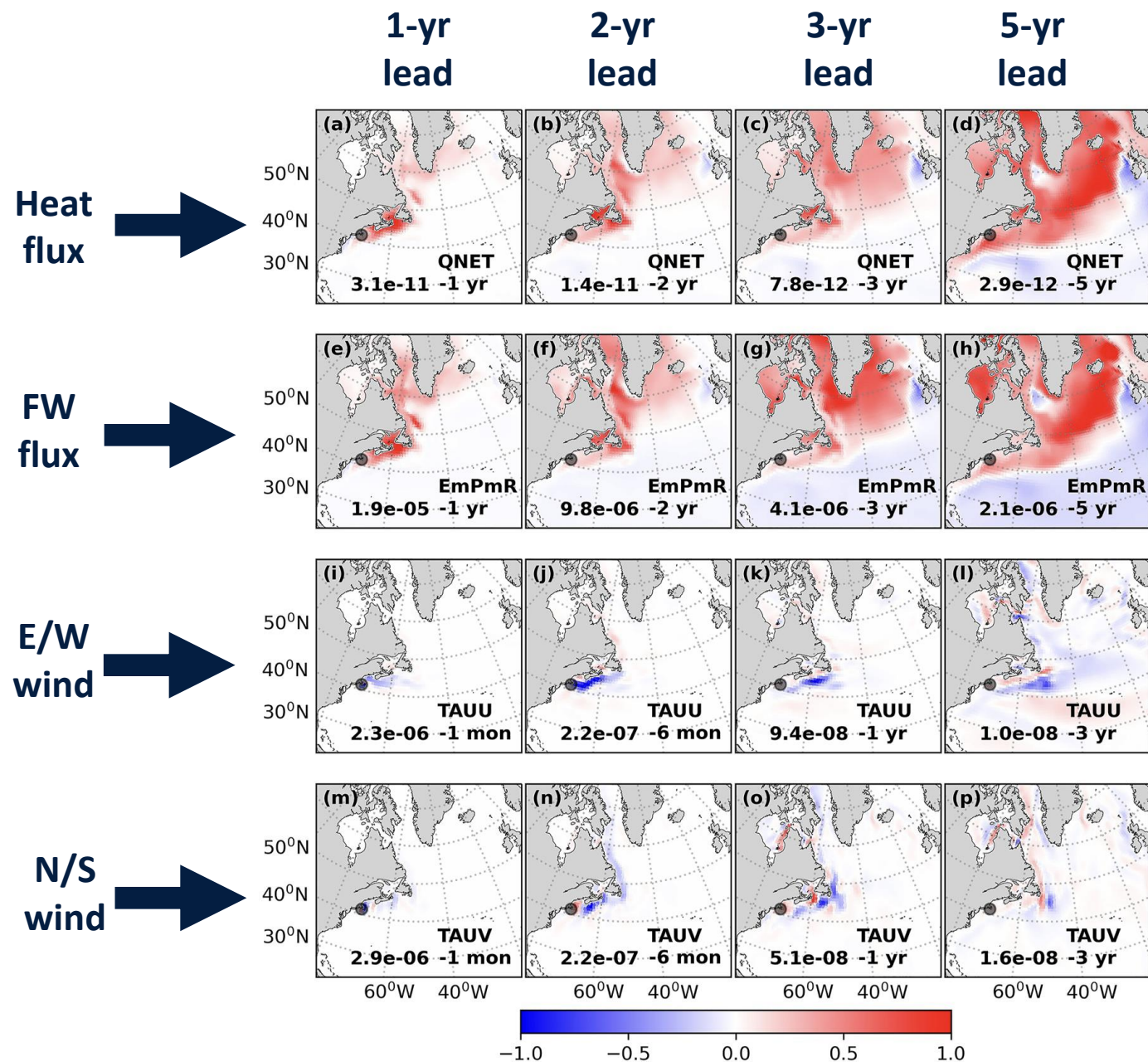
ECCO vignettes: closed budget analyses

What drives decadal variability in western tropical Pacific sea level?



ECCO vignettes: adjoint sensitivity analyses

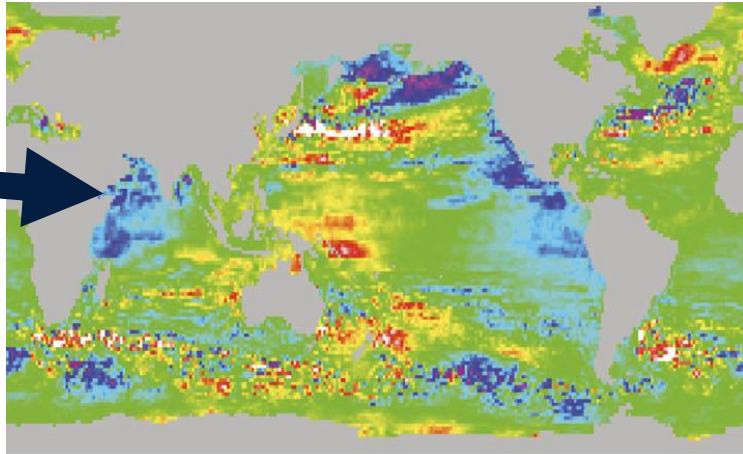
What drives sea-level
variability on Nantucket?



ECCO vignettes: passive tracer experiments

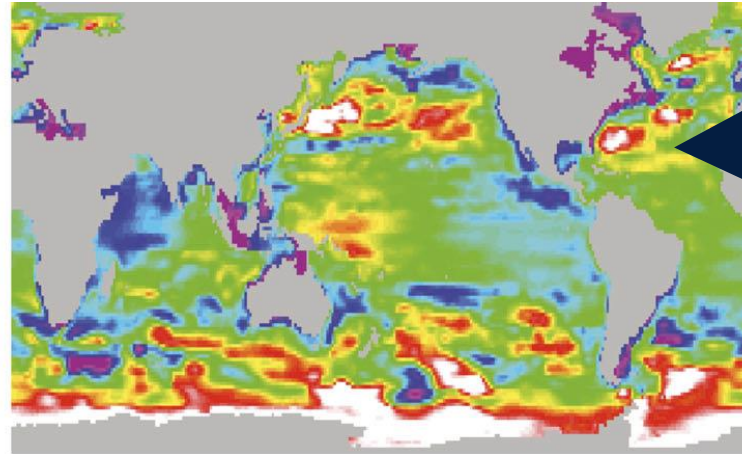
Relative roles of internal diabatic sources and internal redistribution

Observed trends '93-'04



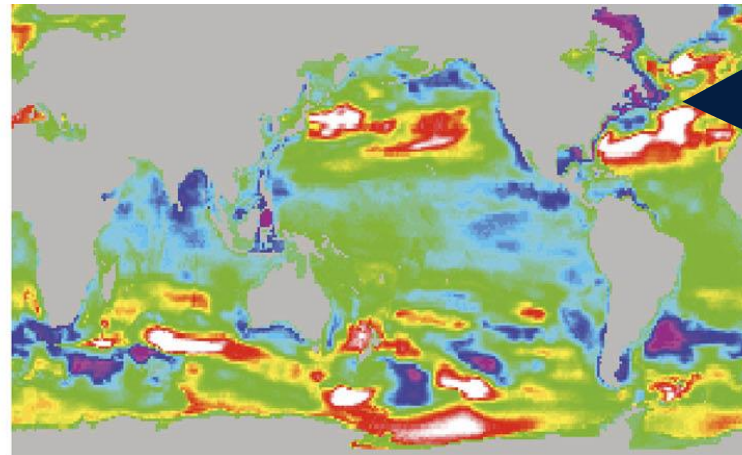
(mm/yr)
12
0
-12

Modeled trends '93-'04
(ECCO v2.216)



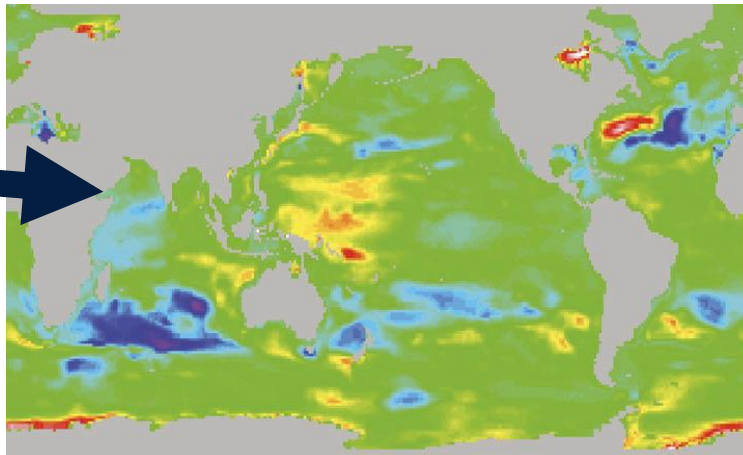
(mm/yr)
12
0
-12

Modeled steric trends from
water mass redistribution



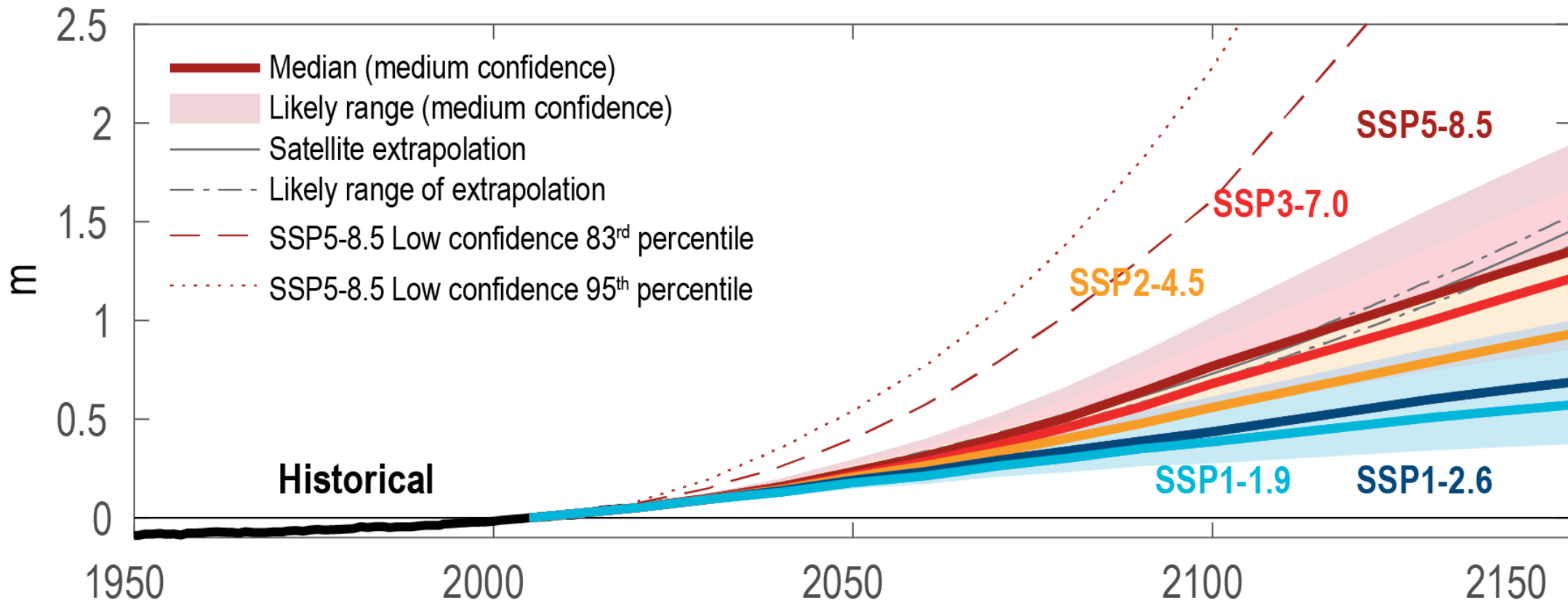
-12

Modeled steric trends from
external diabatic sources



**Sea level will continue rising
for centuries and even millennia**

Global-mean sea level



IPCC 6th Assessment Report Sea Level Projections

Median projections of global and regional sea level rise, relative to a 1995-2014 baseline.

[About the data](#)

Data

- ☒ Scenario
- ☐ Warming Level

Process

Total Sea Level

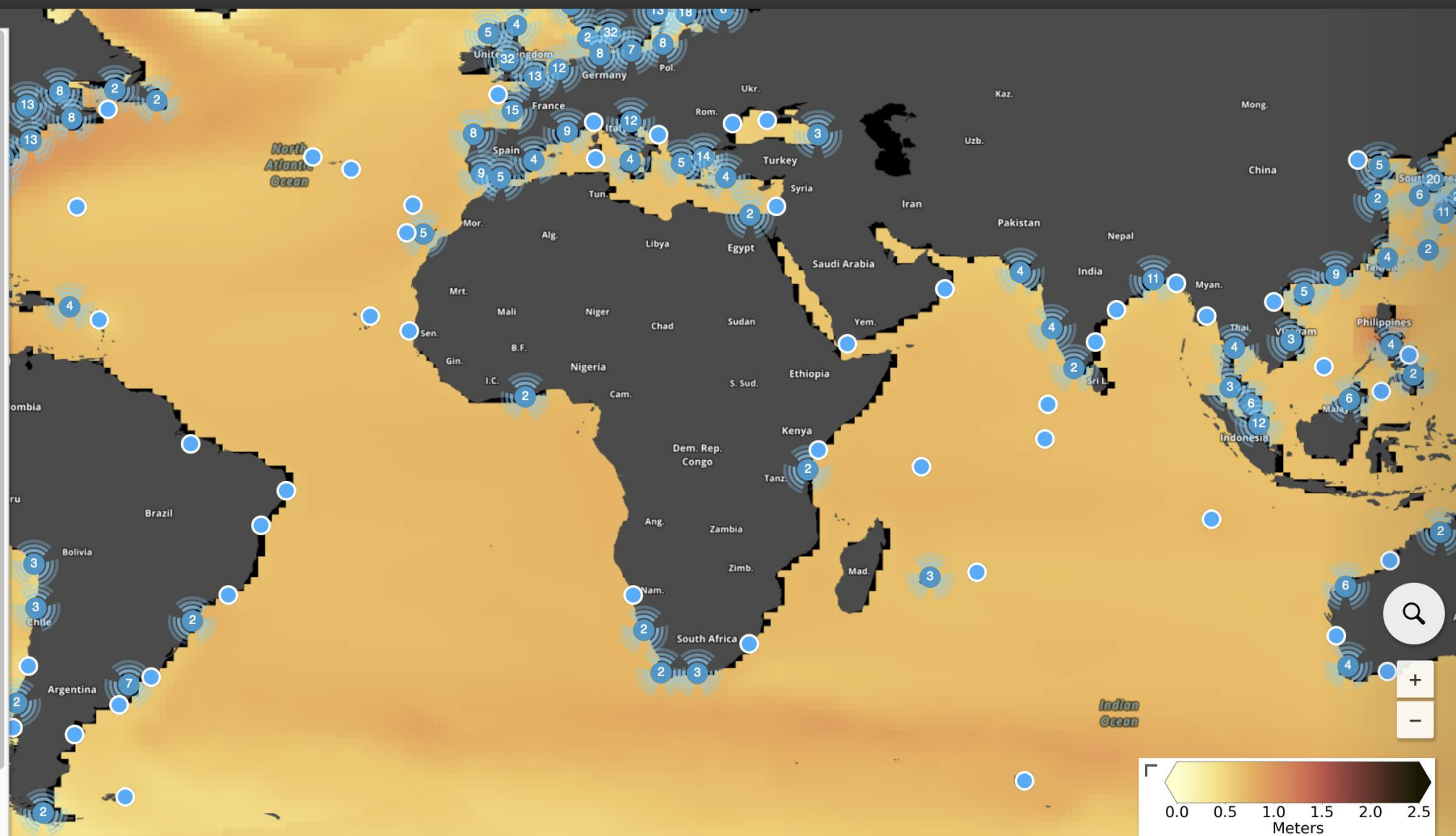
Decades

2100

Scenario

SSP3-7.0

UPDATE MAP



The diagram consists of three teal circles of increasing size, arranged in a triangular pattern. Each circle contains white text indicating a time period and a corresponding sea-level rise range. The circles are positioned at the top-left, bottom-center, and top-right of the main content area.

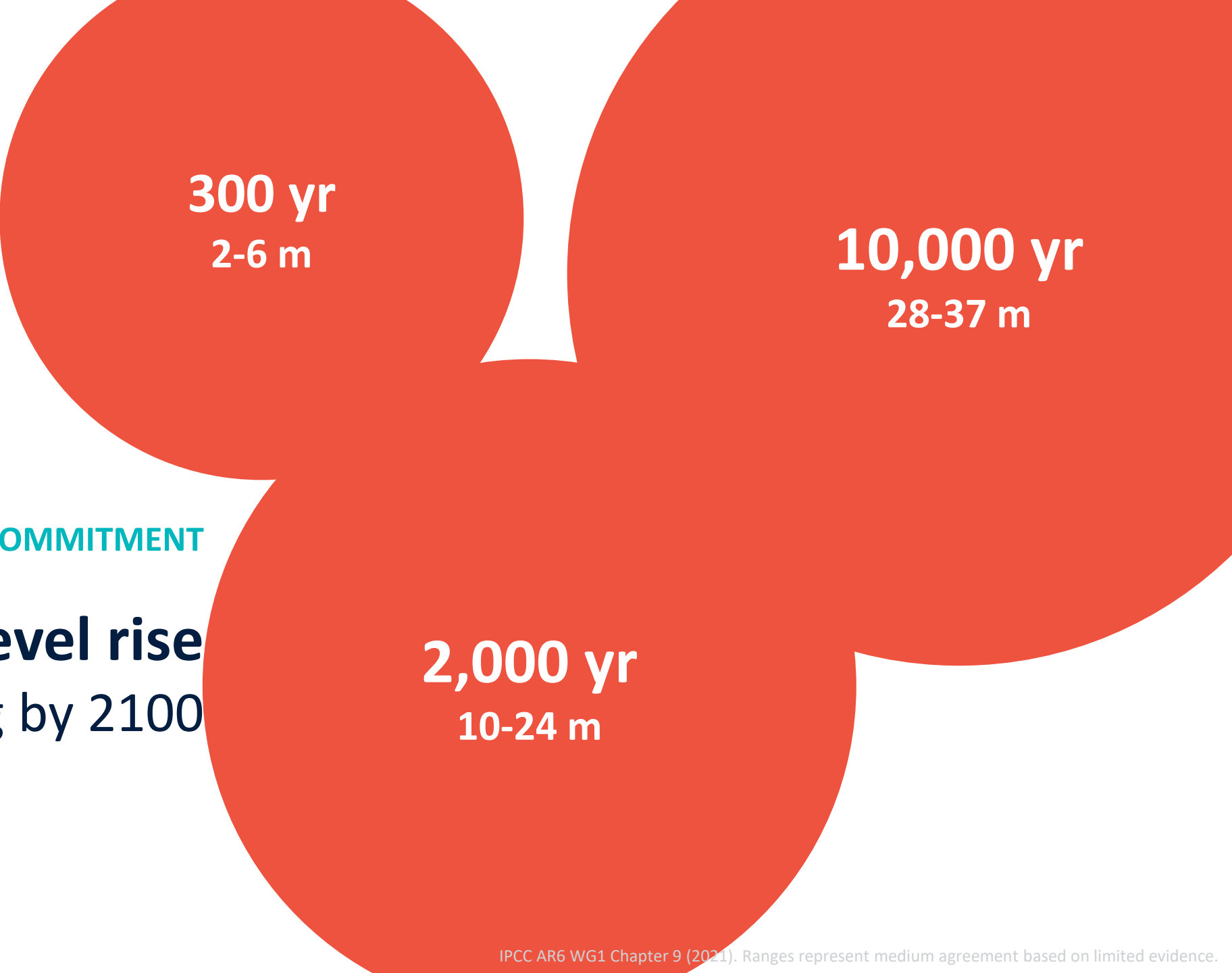
300 yr
1-3 m

10,000 yr
6-7 m

LONGTERM COMMITMENT

Future sea-level rise
1.5°C warming by 2100

2,000 yr
2-3 m



300 yr
2-6 m

10,000 yr
28-37 m

LONGTERM COMMITMENT

Future sea-level rise
5.0°C warming by 2100

2,000 yr
10-24 m

**You should consider contributing
to sea level science!**

NASA Sea Level Change Team

- Deepen knowledge of Earth system interactions that influence relative sea level change
- Deliver improved estimates of future sea level effects that integrate across the Earth system processes
- Contribute to National and global science foundations that support sea level and coastal resilience decision-making



NASA Sea Level Change Team

- Planned N-SCLT early-career researcher network
- Planned N-SLCT summer school 2026
- Get in touch! (cpiecuch@who.edu)

Summary

Sea-level rise is a whole-Earth process

Current rates of sea-level rise are exceptional

Sea level is coupled to ocean circulation and climate

NASA data and models (including ECCO!) have revolutionized our understanding of sea-level change

You should contribute to sea-level science!